



THE INSTITUTE FOR  
MOLECULAR  
ENGINEERING



# Computational Mesoscale Materials Problems

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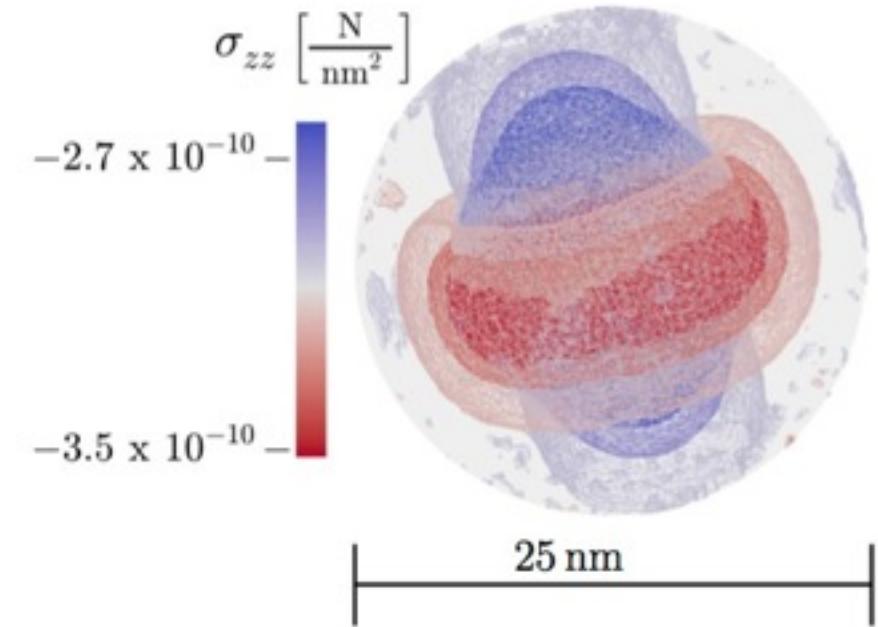
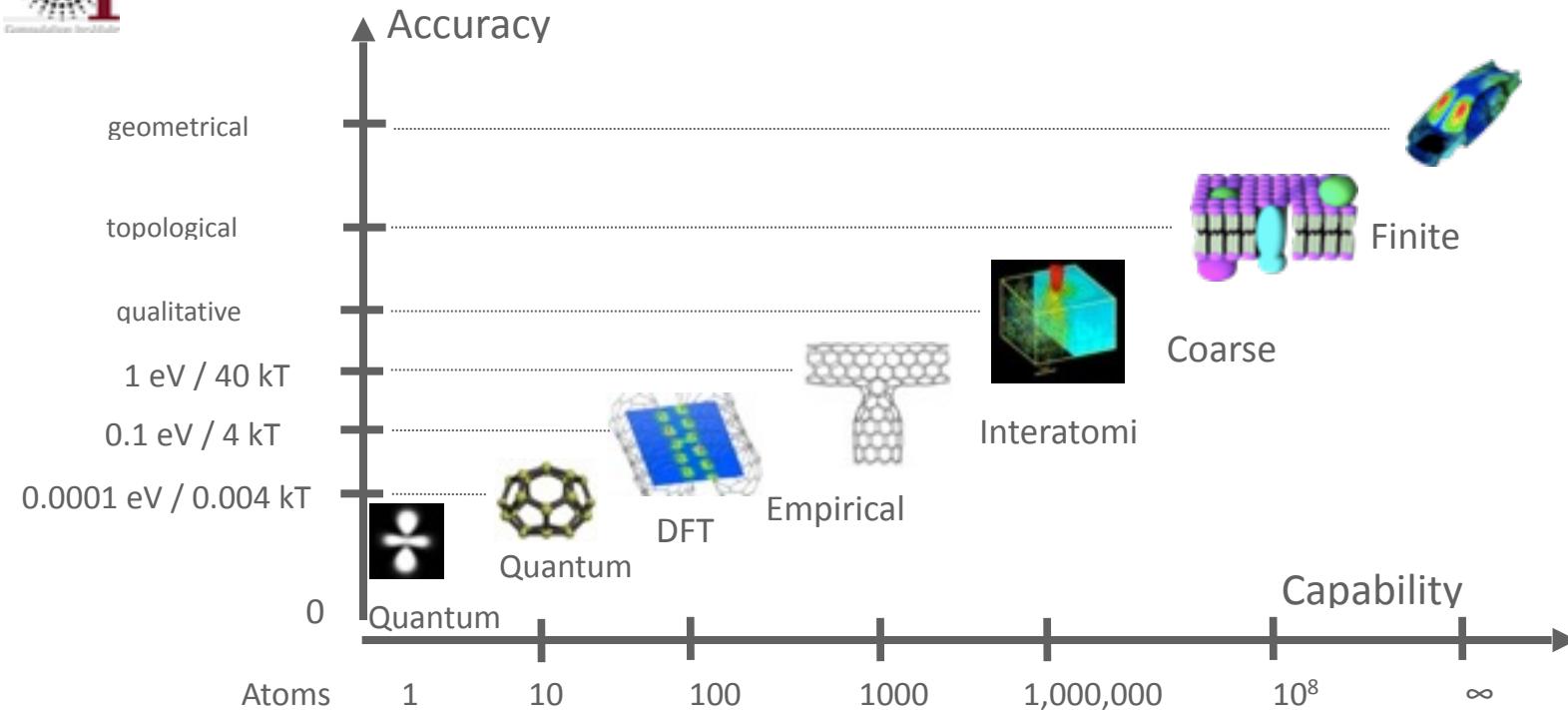
the de Pablo Lab, IME U.Chicago

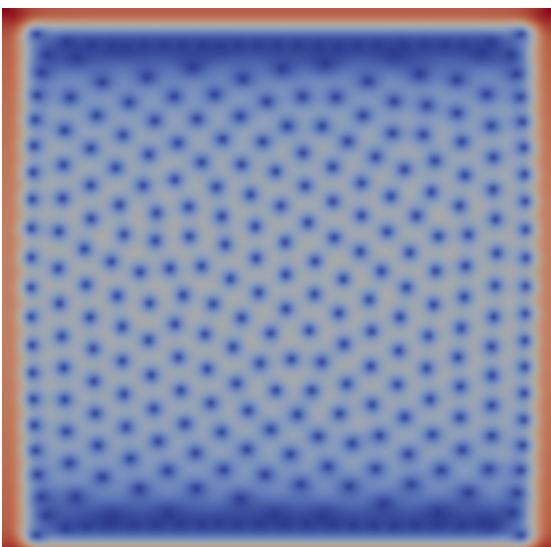
and many others!

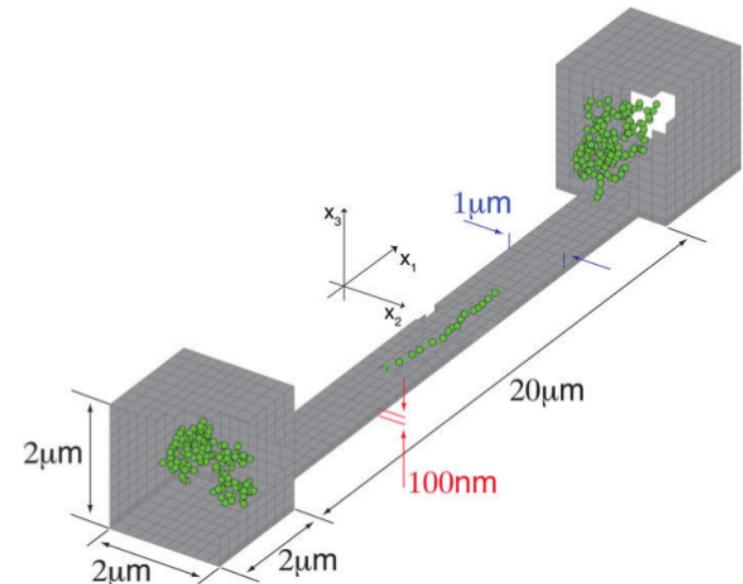
PETSc



# Discrete-continuum models of mesoscale phenomena



- 
- Continuum and continuum-particle methods
  - Methods/code development:
    - High performance simulation
    - Optimization/sensitivity
    - Visualization



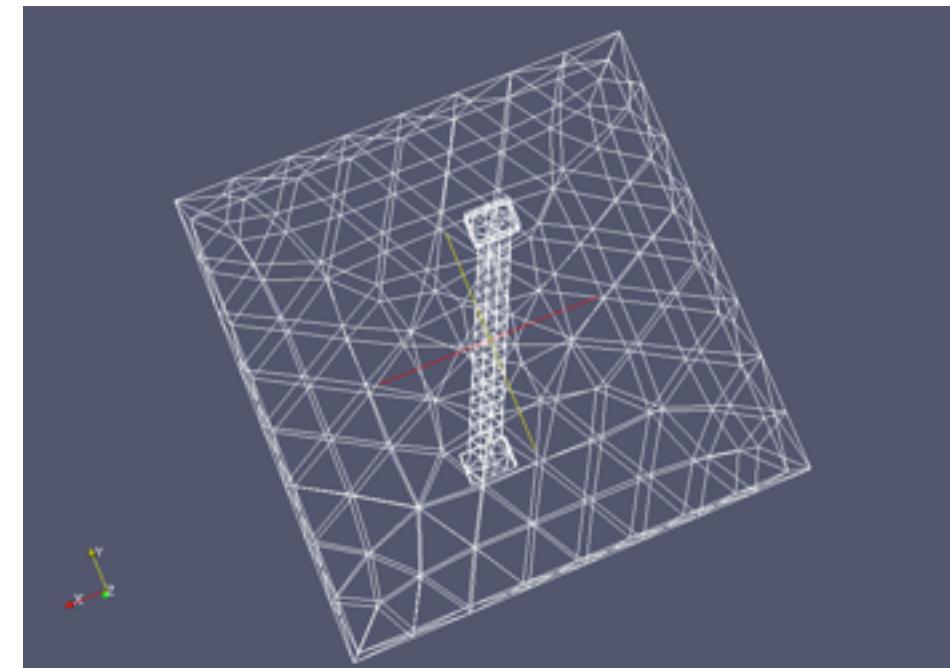
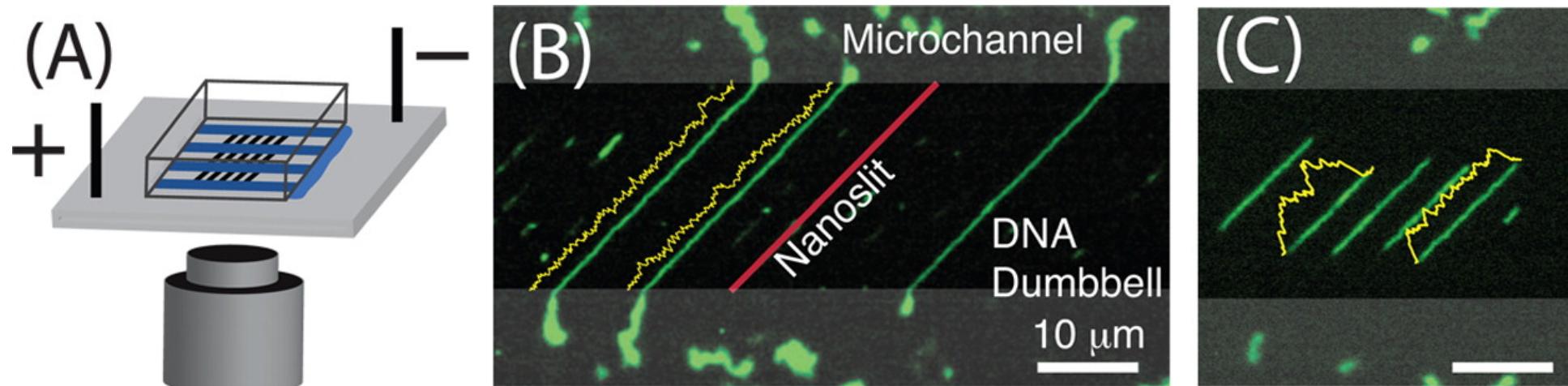


# Soft matter: Institute for Molecular Engineering



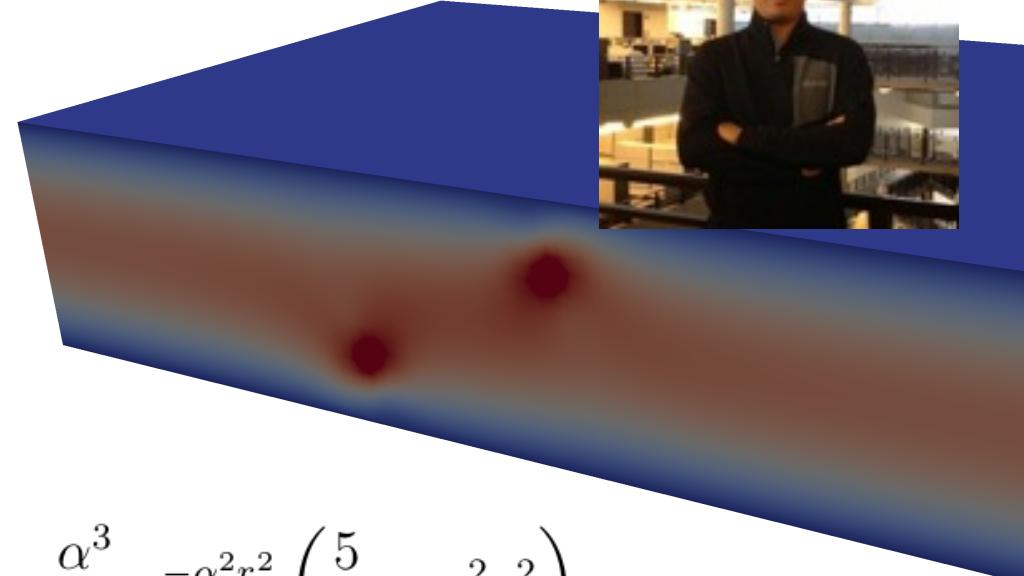
# Translocation of DNA through nanochannels/nanoslits

- Multiphysics
  - Continuum:
    - Electrostatics
    - Hydrodynamics (Stokes)
    - Counter-ions drift-diffusion (Nernst-Planck)
  - Discrete:
    - Excluded volume (Lennard-Jones)
    - Nonlinear spring
  - Continuum-discrete:
    - Capture singular charges/forces
- “Geometry”
  - Separation of spatial scales
  - “Irregular” boundary
- Outer-loop
  - Long-time noise-driven evolution
  - Shape optimization



# Resolving point singularities

- GGEM: General Geometry Ewald-like Method
  - $O(N)$  via alpha tuning
  - PRL 98, 140602 (2007), J. Hernandez-Ortiz, J. de Pablo, M. Graham
  - Serial workhorse of particle simulations
  - Slow: weeks to months for physically relevant runs
- Parallelization based on PETSc/libMesh (Xujun Zhao)
  - Particle-particle computation may be suitable for GPU/MIC



$$-\nu \Delta u + \nabla p = \sum_i f_i \delta(x - x_i), \quad \nabla \cdot u = 0, \quad u|_{\Gamma} = \bar{u}$$

$$g_{\alpha}(x) = \frac{\alpha^3}{\pi^{3/2}} e^{-\alpha^2 r^2} \left( \frac{5}{2} - \alpha^2 r^2 \right)$$

$$\delta(x - x_i) = g_{\alpha}(x - x_i) + \underbrace{(\delta(x - x_i) - g_{\alpha}(x - x_i))}_{\hat{\delta}_{\alpha}(x - x_i)}$$

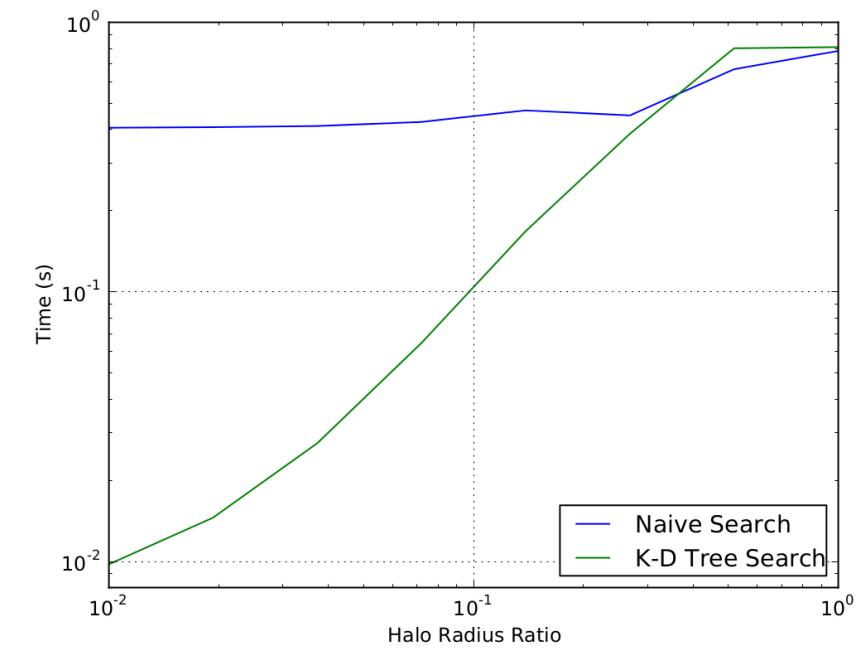
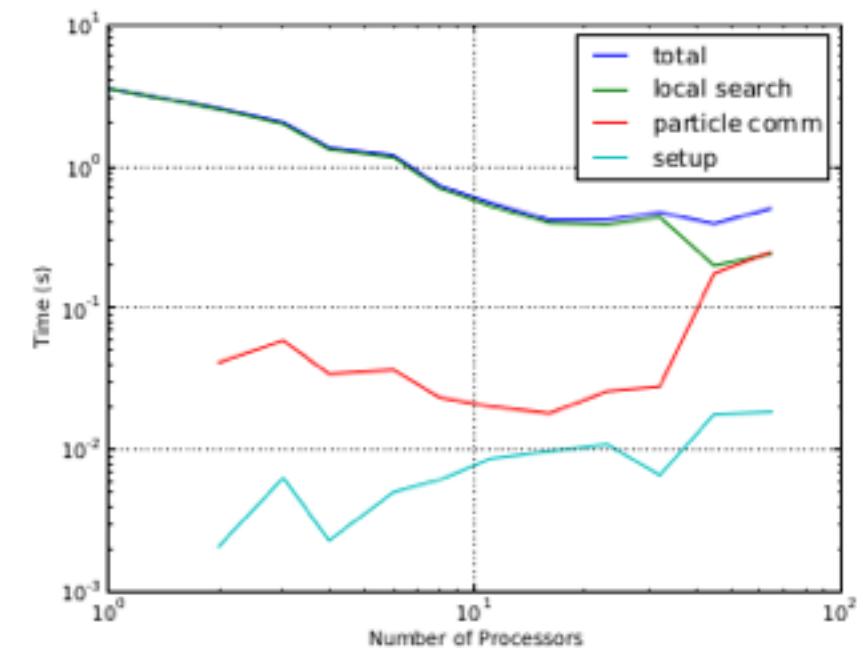
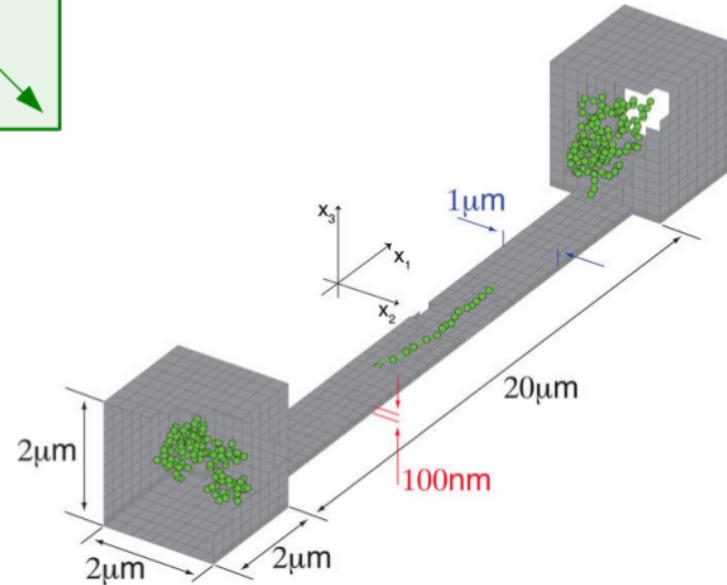
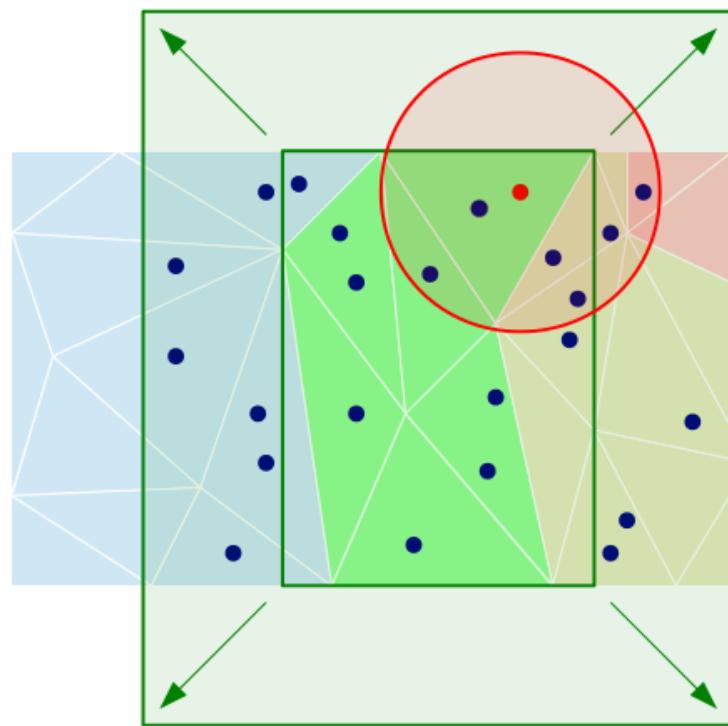
$$-\nu \Delta \hat{G}_{\alpha} + \nabla \hat{P}_{\alpha} = \sum_i f_i \hat{\delta}_{\alpha}(x - x_i)$$

$$-\nu \Delta u_l + \nabla p_l = \sum_i f_i g_{\alpha}(x - x_i), \quad \nabla u_l = 0, \quad u_l|_{\Gamma} = \bar{u} - \hat{u}|_{\Gamma}$$

$$G_{\alpha}(x) = \frac{1}{8\pi\nu} \left( I - \frac{xx^T}{r} \right) \frac{1}{r} \times \underbrace{\text{erfc}(\alpha r)}_{\text{erfcx}(\alpha r)e^{-\alpha^2 r^2}} - \frac{1}{8\pi\nu} \left( I + \frac{xx^T}{r} \right) \frac{2\alpha}{\pi^{1/2}} e^{-\alpha^2 r^2}$$

$$u_s(x) = \sum_i G_{\alpha}(x - x_i) f_i$$

# Particles-mesh



# Preconditioned Stokes Solver

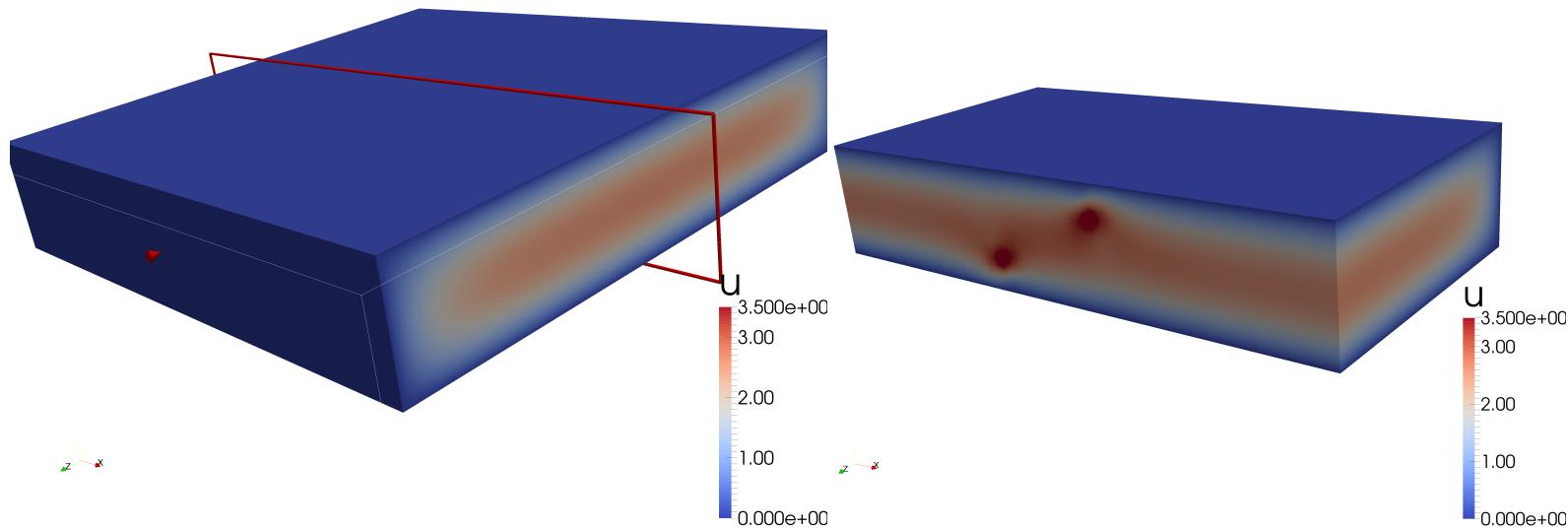
Stokes Equation:

$$\begin{aligned}-\nu \nabla^2 u + \nabla p &= b \\ \nabla \cdot u &= 0\end{aligned}$$

Mixed FEM

Discrete saddle point system:

$$\begin{pmatrix} \mathbf{A} & \mathbf{G} \\ \mathbf{G}^T & \mathbf{0} \end{pmatrix} \begin{pmatrix} \mathbf{u} \\ \mathbf{p} \end{pmatrix} = \begin{pmatrix} \mathbf{f} \\ \mathbf{g} \end{pmatrix}$$



Velocity in x-direction

Clip view at the cross section

# Optimal FieldSplit configuration

	Direct Solver	Iterative Solver					
KSP	Super_LU (dist)	GMRES		TFQMR		GMRES	
PC		ASM		ASM		FIELDSPLIT(with user PC)	
Sub PC		ILU	ASM	ILU	ASM	multiplicative	Schur Complement
Iter #		377	377	219	219	56	43
time	2695.8s	125.8s	130.8	127.8	131.5	98.6	87.1s

- System size : 100 x 20 x 100 micrometers;
- Mesh: 50 x 10 x 50
- Element: Q2-Q1 mixed element
- Total DOF: 671,274
- Relative tol: 1E-9
- Pressure mass matrix in place of S

$$J = \begin{pmatrix} A & B \\ B^T & 0 \end{pmatrix} = \begin{pmatrix} I & 0 \\ B^T A^{-1} & I \end{pmatrix} \begin{pmatrix} A & 0 \\ 0 & -B^T A^{-1} B \end{pmatrix} \begin{pmatrix} I & A^{-1} B \\ 0 & I \end{pmatrix}$$

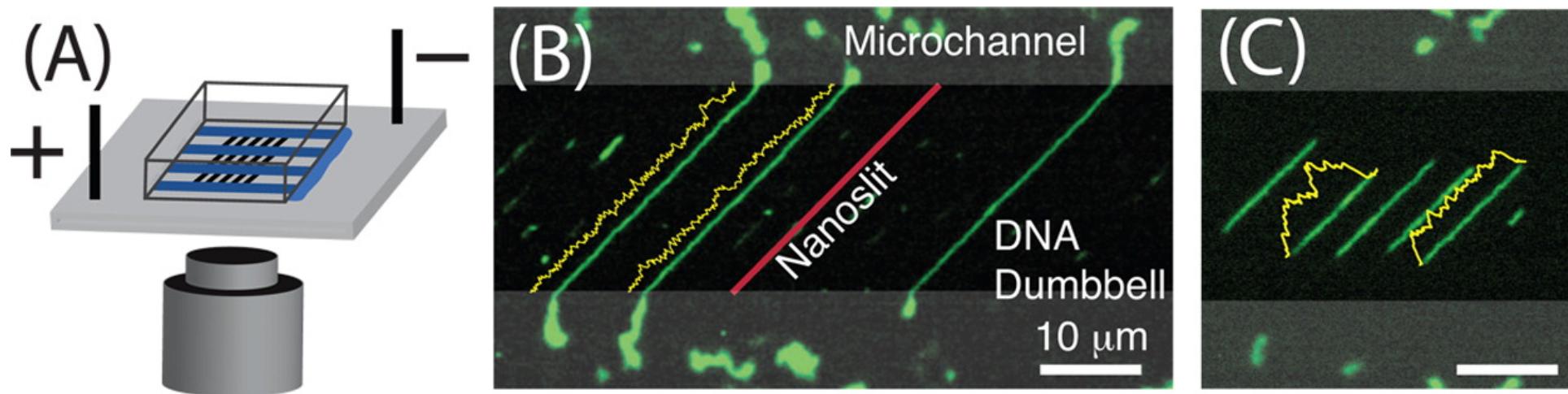
# Optimal FieldSplit configuration

$$J = \begin{pmatrix} A & B \\ B^T & 0 \end{pmatrix} = \begin{pmatrix} I & 0 \\ B^T A^{-1} & I \end{pmatrix} \begin{pmatrix} A & 0 \\ 0 & -B^T A^{-1} B \end{pmatrix} \begin{pmatrix} I & A^{-1} B \\ 0 & I \end{pmatrix}$$

- Can we find this optimal configuration automatically?
    - KSP(A):tol1, KSP\_INNER(A): tol2,KSP(S):tol3
    - Uses derivative-free optimization (POUNDERS) over tol1,tol2,tol3
      - Limit: **500** total evaluations (Stokes solves), **17 hours**
      - 212 points over 7 local optimization runs and 288 points randomly sampled over the domain.
      - time-to-evaluate the starting points for the 6 completed local optimization:
      - 282.6, 291.5, 276.0, 271.5, 288.5, 294.7
      - These are 6 best randomly sampled points, the corresponding minima had solve time
      - 235.2, 282.2, 271.3, 256.0, 286.8, 270.6
      - So the improvement percentages are  
16.8%, 3.2%, 1.7%, 5.7%, 0.6%, 8.2%, 0.4%
- Mean evaluation times for the 288 sample points: 407.2. Minimum found is 42% better.

Discrete choice (e.g., replacing S by Mp) requires more work

# Correlation matrix



- Very long-time simulation
- BdW by far most expensive
- Computed by Chebyshev approximation
- SLEPc spectral estimate, lagged
- Can we do better?
- Use Krylov space of M?
- H-matrix representation of M?

$$dx_i = u(x_i) + B_{ij}dW_j$$

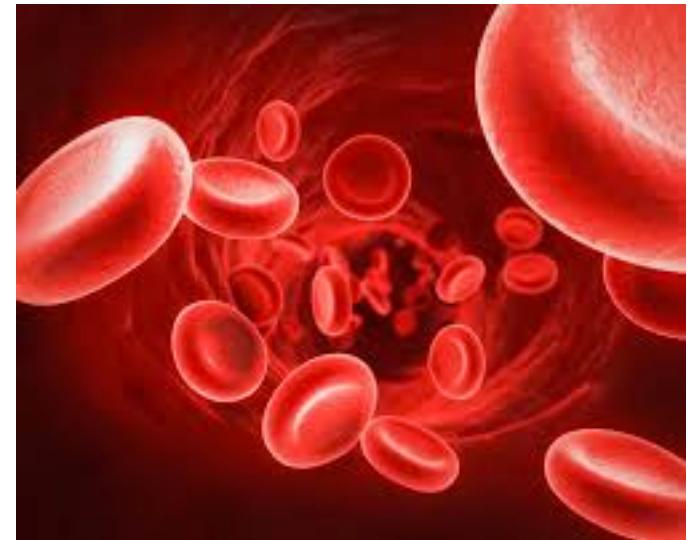
$$u_i = M_{ij}f_j$$

$$M : f_i \rightarrow f(x) = \sum_i f_i \delta(x - x_i) \rightarrow \text{Stokes} \rightarrow u(x) \rightarrow u(x_i)$$

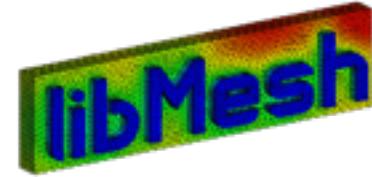
$$B = \sqrt{k_B T M}$$

# Future (nascent) directions

- Extended particles
- Singular interfaces/boundaries
  - forces
  - charges
- GGEM not always applicable:
  - Boundary integral operator/equation formulations
  - Accelerated by FMM
  - In parallel
  - Take advantage of accelerators (GPU, etc.)?
  - Same for particles?



# Thermoelastic Contact

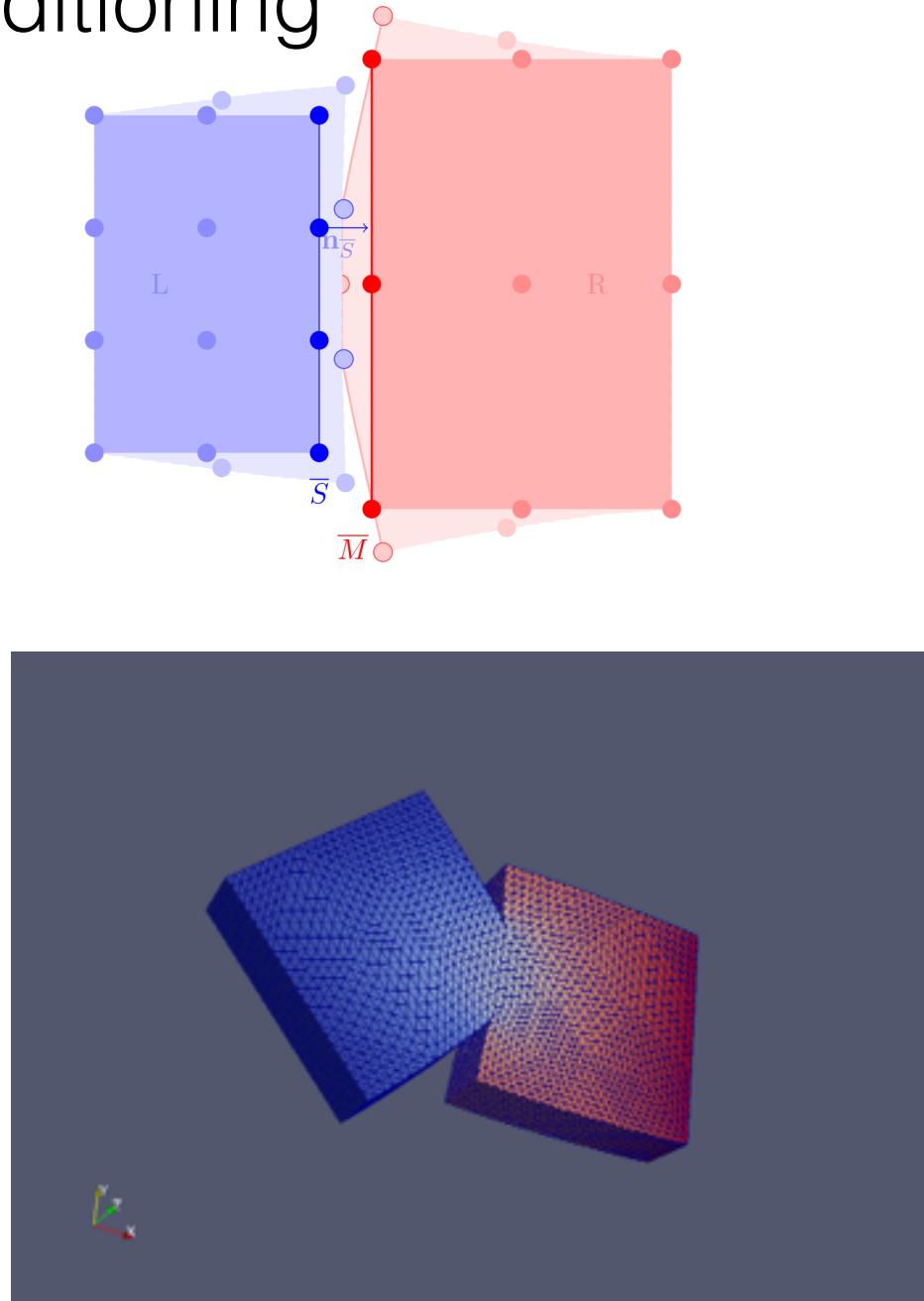


# Contact: FieldSplit preconditioning

$$\begin{array}{c}
 \mathbf{u}_L \quad \mathbf{u}_S \quad \mathbf{u}_M \quad \mathbf{u}_R \quad \lambda \\
 \left( \begin{array}{ccccc} K_{LL} & K_{LS} & 0 & 0 & 0 \\ K_{SL} & K_{SS} & 0 & 0 & I \\ 0 & 0 & K_{MM} & K_{MR} & -I \\ 0 & 0 & K_{RM} & K_{RR} & 0 \\ 0 & I & -I & 0 & 0 \end{array} \right) \begin{bmatrix} \delta \mathbf{u}_L \\ \delta \mathbf{u}_S \\ \delta \mathbf{u}_M \\ \delta \mathbf{u}_R \\ \delta \lambda \end{bmatrix} = \\
 \begin{bmatrix} \mathbf{f}_L - K_{LL} \mathbf{u}_L^0 & -K_{LS} \mathbf{u}_S^0 \\ \mathbf{f}_S - K_{SL} \mathbf{u}_L^0 & -K_{SS} \mathbf{u}_S^0 - \lambda^0 \\ \mathbf{f}_M - K_{MM} \mathbf{u}_M^0 - K_{MR} \mathbf{u}_R^0 + \lambda^0 \\ \mathbf{f}_R - K_{RM} \mathbf{u}_M^0 - K_{RR} \mathbf{u}_R^0 \\ \mathbf{x}_M - \mathbf{x}_S + (\mathbf{u}_M^0 - \mathbf{u}_S^0) \end{bmatrix}
 \end{array}$$

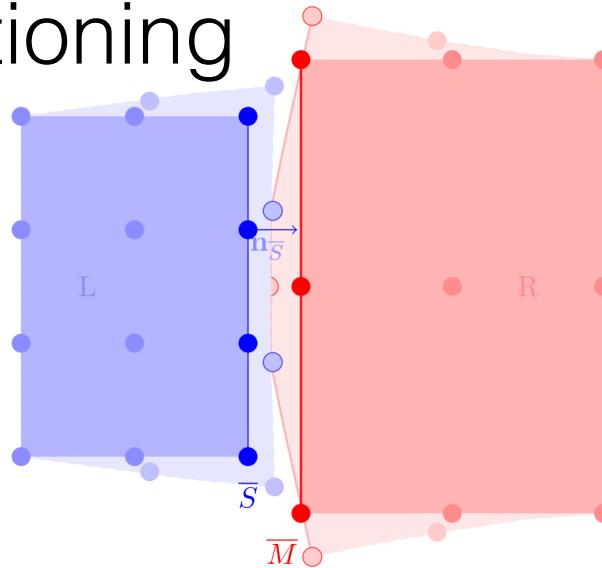
$$\begin{aligned}
 f(x) + \lambda^T B(x) &= 0 \\
 0 \leq \lambda \perp g(x) &\geq 0 \\
 B(x) &= \nabla g(x)
 \end{aligned}$$

$$\begin{pmatrix} A & B \\ B^T & 0 \end{pmatrix}$$



# Contact: FieldSplit preconditioning

$$\begin{array}{cccccc} & \lambda & \mathbf{u}_S & \mathbf{u}_L & \mathbf{u}_M & \mathbf{u}_R \\ \mathbf{u}_S & \left( \begin{array}{cccccc} I & K_{SS} & : & K_{SL} & 0 & 0 \\ 0 & I & : & 0 & -I & 0 \\ \dots & \vdots & & \ddots & & \vdots \\ 0 & K_{LS} & : & K_{LL} & 0 & 0 \\ -I & 0 & : & 0 & K_{MM} & K_{MR} \\ 0 & 0 & : & 0 & K_{RM} & K_{RR} \end{array} \right) & \left[ \begin{array}{c} \delta\lambda \\ \delta\mathbf{u}_S \\ \dots \\ \delta\mathbf{u}_L \\ \delta\mathbf{u}_M \\ \delta\mathbf{u}_R \end{array} \right] \end{array}$$



- General VIs

$$\begin{array}{cccccc} & \lambda & \mathbf{u}_S & : & \mathbf{u}_L & \mathbf{u}_M & \mathbf{u}_R \\ \mathbf{u}_S & \left( \begin{array}{cccccc} I & K_{SS} & : & K_{SL} & 0 & 0 \\ 0 & I & : & 0 & -I & 0 \\ \dots & \vdots & & \ddots & & \vdots \\ 0 & 0 & : & K_{LL} & K_{LS} & 0 \\ 0 & 0 & : & K_{SL} & K_{MM} + K_{SS} & K_{MR} \\ 0 & 0 & : & 0 & K_{RM} & K_{RR} \end{array} \right) & \left[ \begin{array}{c} \delta\lambda \\ \delta\mathbf{u}_S \\ \dots \\ \delta\mathbf{u}_L \\ \delta\mathbf{u}_M \\ \delta\mathbf{u}_R \end{array} \right] \end{array}$$

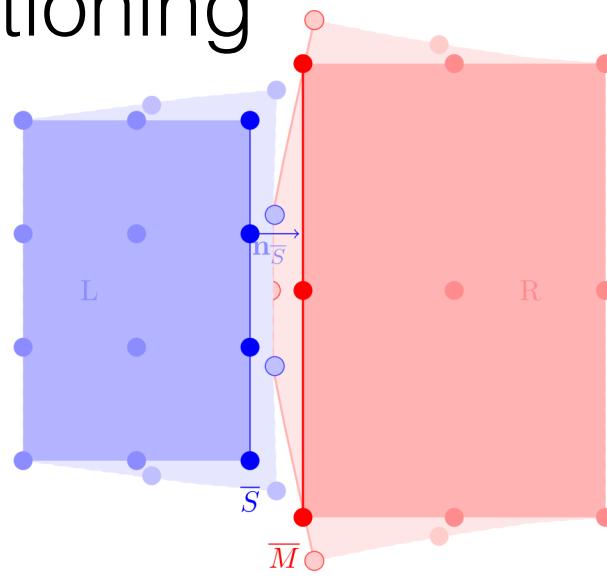
$$\begin{pmatrix} A & B \\ B^T & 0 \end{pmatrix}$$

- Primal reduced system
- Also phasefield models (volume fraction constraint)
- On-going work with Todd Munson, Jason Sarich, Fande Kong



# Contact: FieldSplit preconditioning

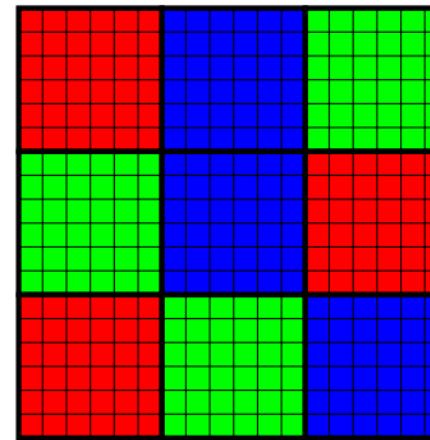
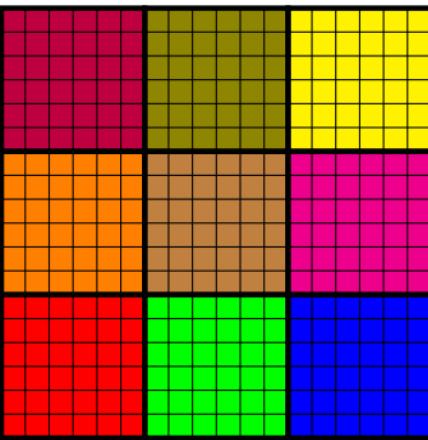
$$\begin{array}{cccccc}
 & \lambda & \mathbf{u}_S & \mathbf{u}_L & \mathbf{u}_M & \mathbf{u}_R \\
 \hline
 \mathbf{u}_S & \left( \begin{array}{ccccc} I & : & K_{SS} & K_{SL} & 0 & 0 \\ \vdots & & \ddots & \ddots & \ddots & \ddots \\ \lambda & 0 & : & I & 0 & -I & 0 \\ \mathbf{u}_L & 0 & : & K_{LS} & K_{LL} & 0 & 0 \\ \mathbf{u}_M & -I & : & 0 & 0 & K_{MM} & K_{MR} \\ \mathbf{u}_R & 0 & : & 0 & 0 & K_{RM} & K_{RR} \end{array} \right) & \left[ \begin{array}{c} \delta\lambda \\ \dots \\ \delta\mathbf{u}_S \\ \delta\mathbf{u}_L \\ \delta\mathbf{u}_M \\ \delta\mathbf{u}_R \end{array} \right]
 \end{array}$$



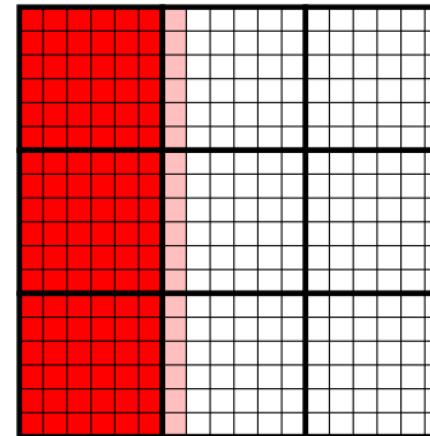
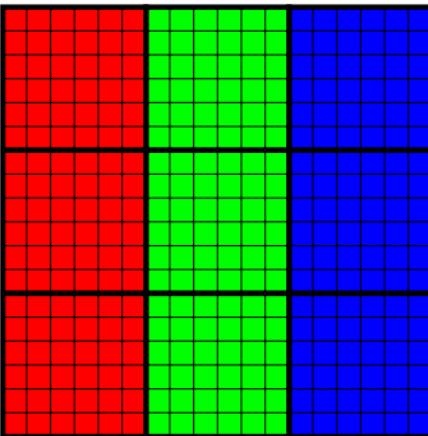
$$\begin{array}{cccccc}
 & \lambda & \mathbf{u}_S & \mathbf{u}_L & \mathbf{u}_M & \mathbf{u}_R \\
 \hline
 \mathbf{u}_S & \left( \begin{array}{ccccc} I & : & K_{SS} & K_{SL} & 0 & 0 \\ \vdots & & \ddots & \ddots & \ddots & \ddots \\ \lambda & 0 & : & I & 0 & -I & 0 \\ \mathbf{u}_L & 0 & : & K_{LS} & K_{LL} & 0 & 0 \\ \mathbf{u}_M & 0 & : & K_{SS} & K_{SL} & K_{MM} & K_{MR} \\ \mathbf{u}_R & 0 & : & 0 & 0 & K_{RM} & K_{RR} \end{array} \right) & \left[ \begin{array}{c} \delta\lambda \\ \dots \\ \delta\mathbf{u}_S \\ \delta\mathbf{u}_L \\ \delta\mathbf{u}_M \\ \delta\mathbf{u}_R \end{array} \right]
 \end{array}$$

- Preconditioner?
- PCASM is remarkably robust
- Limited to small subdomains

# PCGASM



- Multirank subdomains
- Hierarchical partitioning
- Multirank MatIncreaseOverlap()
- On-going work with Fande Kong



# Geometric multigrid support for libMesh

# Phasefield crystal



- Phasefield Crystal (PFC) is used in problems where atomic effects are needed, but on a larger time scale, typically microseconds.
- PFC is a type of Density Functional Theory, which requires minimizing the energy functional:

$$\frac{\beta \Delta F}{\rho_0} = \int dr ([1 + n(r)] \ln[1 + n(r)] - n(r)) \\ - \frac{\rho_0}{2} \int \int dr_1 dr_2 n(r_1) c^{(2)}(|r_1 - r_2|) n(r_2)$$

INL LDRD: M. Tonks, Y. Zhang  
U.Michigan: K. Thornton's group  
D. Massatt: 2014 Argonne Givens Fellow

- The Fourier Transform of  $c^{(2)}$  can be approximated by a Rational Function Fit,  $\rho_0 \hat{c}_{RFF}^{(2)} = \sum_{j=1}^m \left[ \frac{A_j}{k^2 + \alpha_j} + \frac{A_j^*}{k^2 + \alpha_j^*} \right]$
- Taking the inverse Fourier Transform, one finds:

$$\rho_0 \int c^{(2)}(|r_1 - r_2|) n(r_2) dr_2 = \sum_j [L_j(r) + L_j^*(r)]$$

Where  $L_j$  defined to be the solution to  $-\Delta L_j(r) + \alpha_j L_j(r) = A_j n(r)$ ,  
and  $-\Delta L_j^*(r) + \alpha_j^* L_j^*(r) = A_j^* n(r)$ .

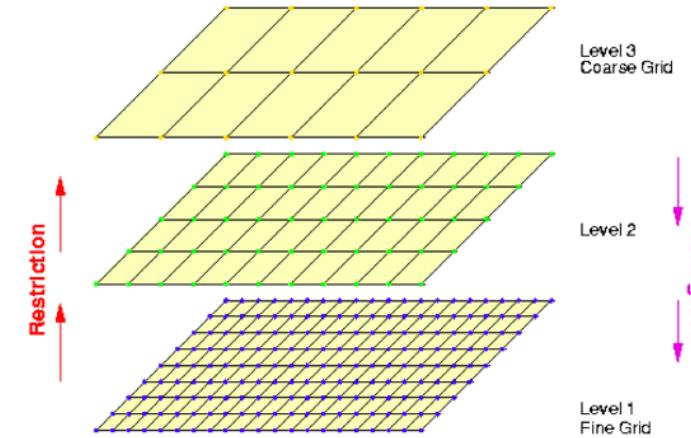
## Helmholtz Equation

$$-\Delta u + \gamma u = f$$

$$A^h u^h = f^h$$

### Difficulties of Solving Helmholtz

- ① GMRES Block Jacobi or Additive Schwarz Method (ASM) preconditioning have poor convergence rates
- ② Geometric Multigrid diverges
- ③ Algebraic Multigrid (AMG) using Hypre BoomerAMG has too expensive a setup time



[Luksch]

## Helmholtz Eigenvalues

$$-\frac{d^2}{dx^2} u - k^2 u = f, \quad A^h u^h = f^h$$

$$\text{Eigenvalues: } \lambda_i = \frac{4}{h^2} \sin^2\left(\frac{\pi i h}{2}\right) - k^2$$

- Prolongation generates error dependent on  $(1 - \frac{\lambda^h}{\lambda^H})$ , which makes eigenvalue sign changes problematic, so use GMRES as an outer iteration
- For  $\pi/5 \leq kh \leq 2 \cos(\pi h/2)$ , damped Jacobi smoothers have poor convergence, so use GMRES as a smoother on these intermediate levels.

# levels	256 Elements				512 Elements			
	k = 4 $\pi$		k = 8 $\pi$		k = 4 $\pi$		k = 8 $\pi$	
	MG	GMRS	MG	GMRS	MG	GMRS	MG	GMRS
2	6	3	11	4	7	3	6	4
3	25	5	-	6	10	6	-	5
4	-	6	-	8	-	6	-	7
5	-	7	-	12	-	7	-	8
6	-	10	-	16	-	8	-	12
7	-	11	-	19	-	10	-	17
8	-	12	-	20	-	11	-	19
9	-	12	-	20	-	12	-	19
10					-	12	-	19

For the 3D, we compare using Multigrid with Damped Jacobi Smoothers to adding FGMRES as an outer iteration, and then adding GMRES smoothers to the appropriate intermediate and coarse levels.

Domain: $65 \times 65 \times 65$ , 6 levels of Multigrid			
$\gamma$	MG	FGMRES outer	Elman smoothing
0	5	4	N/A
$-.0606 + .746i$	5	4	N/A
$-3.062 + .7919i$	5	4	N/A
$-10 + i$	5	4	4
$-25 + i$	5	4	4
$-27 + i$	6	5	4
$-28.5 + i$	24	6	6
$-30 + i$	-	6	6
$-50 + i$	-	6	4
$-100 + i$	-	14	8
$-200 + i$	-	54	9
$-300 + i$	-	391	11
$-400 + i$	-	2000+	19

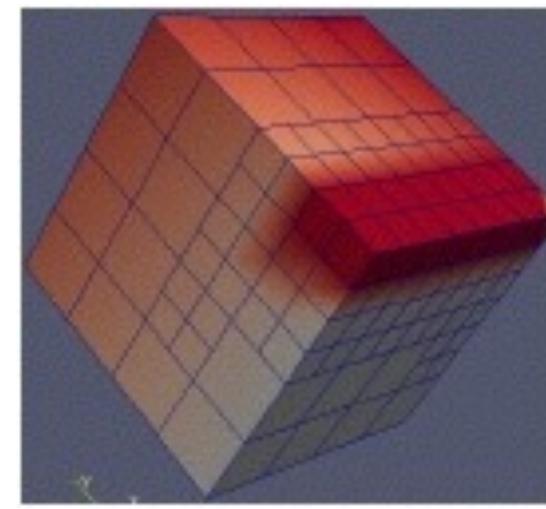
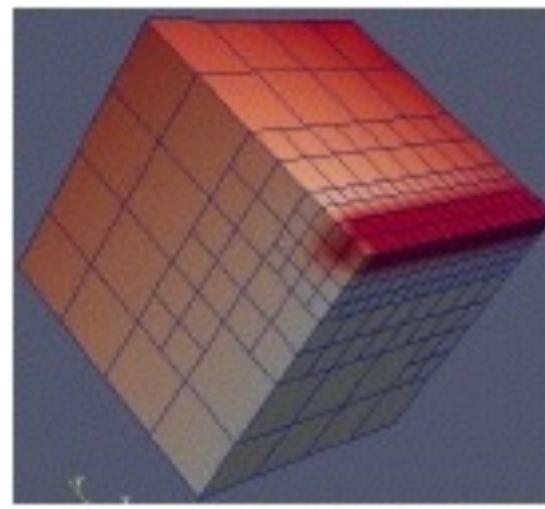
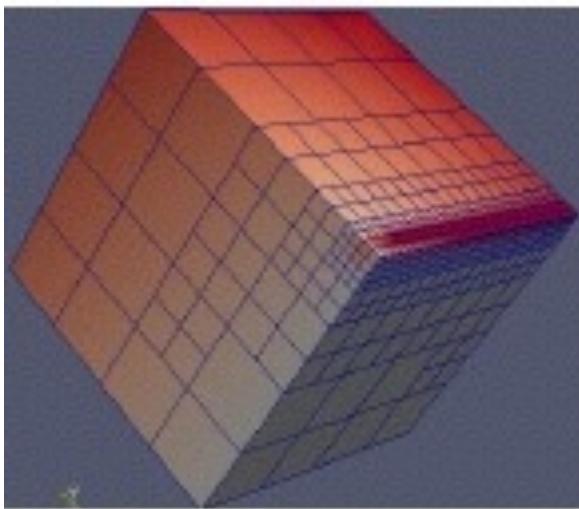
Here we compare Elman's method to GMRES with ASM preconditioner, and to AMG.

Domain: 401 × 401 × 401, 5 levels of Multigrid				
$\gamma$	FGMRES, PC Multigrid	ASM		
-0.0606 + .746i	3	176s	555	2080s
-3.239 + .472i	3	165s	595	2180s
-1.568 + .601i	3	174s	556	2046s
-1.734 + 1.074i	3	168s	574	2113s
-3.062 + .7919i	3	181s	593	2169s
-1.554 - 1.394i	3	170s	572	2087s

Domain: 201 × 201 × 201, 4 levels of Multigrid				
$\gamma$	FGMRES, PC Multigrid	Hypre, BoomerAMG		
-0.0606 + .746i	4	23s	4	357s
-3.239 + .472i	4	24s	4	352s
-1.568 + .601i	4	26s	4	362s
-1.734 + 1.074i	4	27s	4	352s
-3.062 + .7919i	4	28s	4	356s
-1.554 - 1.394i	4	22s	4	351s

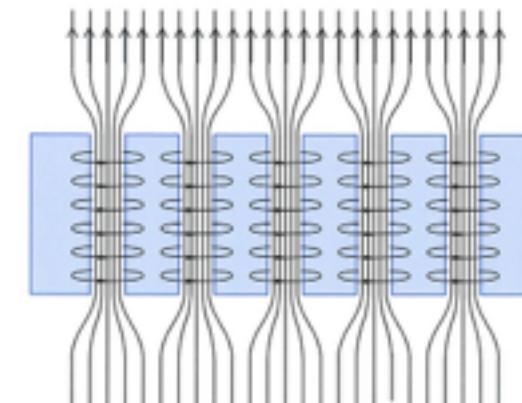
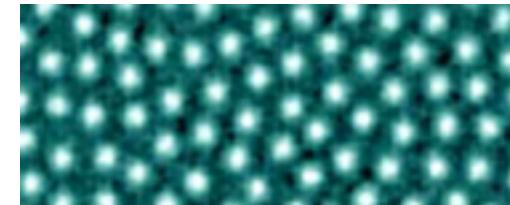
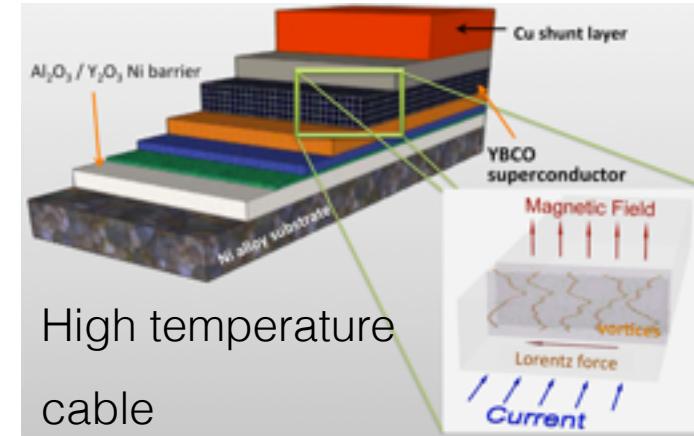
# Multigrid on AMR meshes

- Most interesting problems are not on uniform grids, so we move to unstructured grids.
- We are using Fast Adaptive Composite (FAC) grid refinement since it is simpler to setup in libMesh.
- The Multi-level Adaptive Technique (MLAT) is faster, but harder to implement.



# High temperature type-II superconductors (zero electrical resistance material)

- Magnetic field penetrates the superconductor as quantized fluxes – magnetic vortices
- Vortices are flexible tubes that move, twist, repel, merge.
- Vortices determine *all* the electrodynamic responses of superconductors to electric and magnetic fields
- Vortex moving leads to power dissipation. Vortices can be pinning on non-superconducting defects

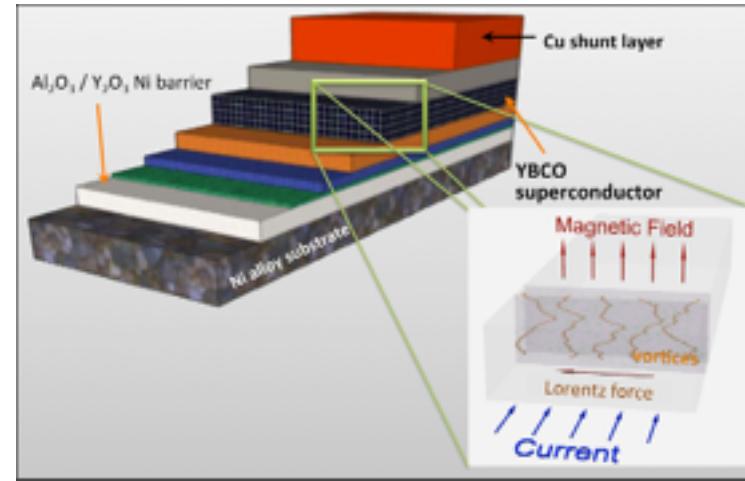


Magnetic vortices

# Lossless energy transport in through superconducting cables



1<sup>st</sup> generation cable  
including insulation &  
cooling ↓



high-current transmission (in urban areas, here NY) ↓



← 2<sup>nd</sup> generation cable  
with illustration of vortex motion  
compact generators &  
motors ↓



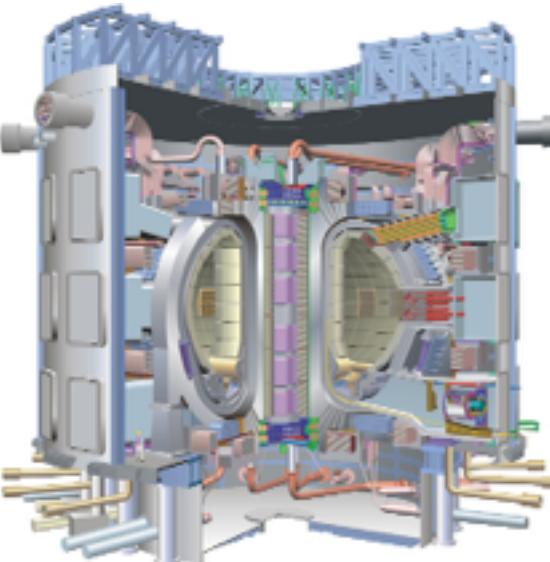
# Other applications



LHC magnets



Maglev trains



ITER magnets



Diagnostic applications (MNR, MRI, ...)

# Superconducting cables



- 5x power capacity of copper in same cross-sectional area
  - Relieve urban power bottleneck in cities and suburbs
- Cables operating at 77 K are technically ready
  - in-grid demonstrations at Copenhagen DK, Albany NY, Long Island NY, Columbus OH, New Orleans LA, Amsterdam

## *Barriers to grid penetration*

- Reduce cost by factor 10 - 100 to compete with copper
- Demonstrate reliable multiyear operation

# Ginzburg-Landau equations

## Time dependent Ginzburg-Landau equations

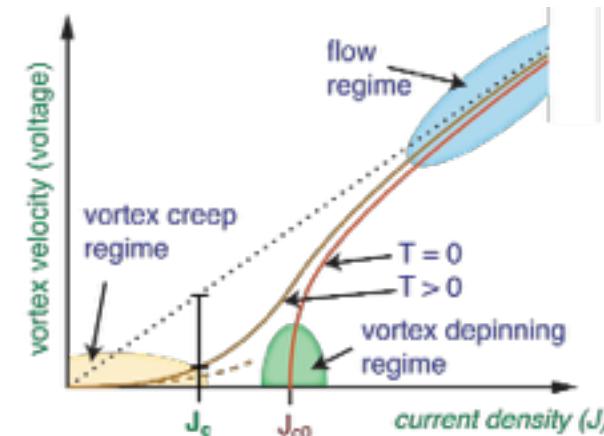
$$\frac{\partial \Psi}{\partial t} = -\frac{\delta \mathcal{F}_{\text{GL}}}{\delta \Psi^*}, \quad \frac{\delta \mathcal{F}_{\text{GL}}}{\delta \mathbf{A}} = 0$$

$$u(\partial_t + i\mu)\psi = \epsilon(\mathbf{r})\psi - |\psi|^2\psi + (\nabla - i\mathbf{A})^2\psi + \zeta(\mathbf{r}, t)$$
$$\kappa^2 \nabla \times (\nabla \times \mathbf{A}) = \mathbf{J}_n + \mathbf{J}_s + \mathcal{I},$$

Total current  $\mathbf{J} = \mathbf{J}_s + \mathbf{J}_n$

$$\mathbf{J} = \text{Im} [\psi^*(\nabla - i\mathbf{A})\psi] - (\nabla\mu + \partial_t \mathbf{A})$$

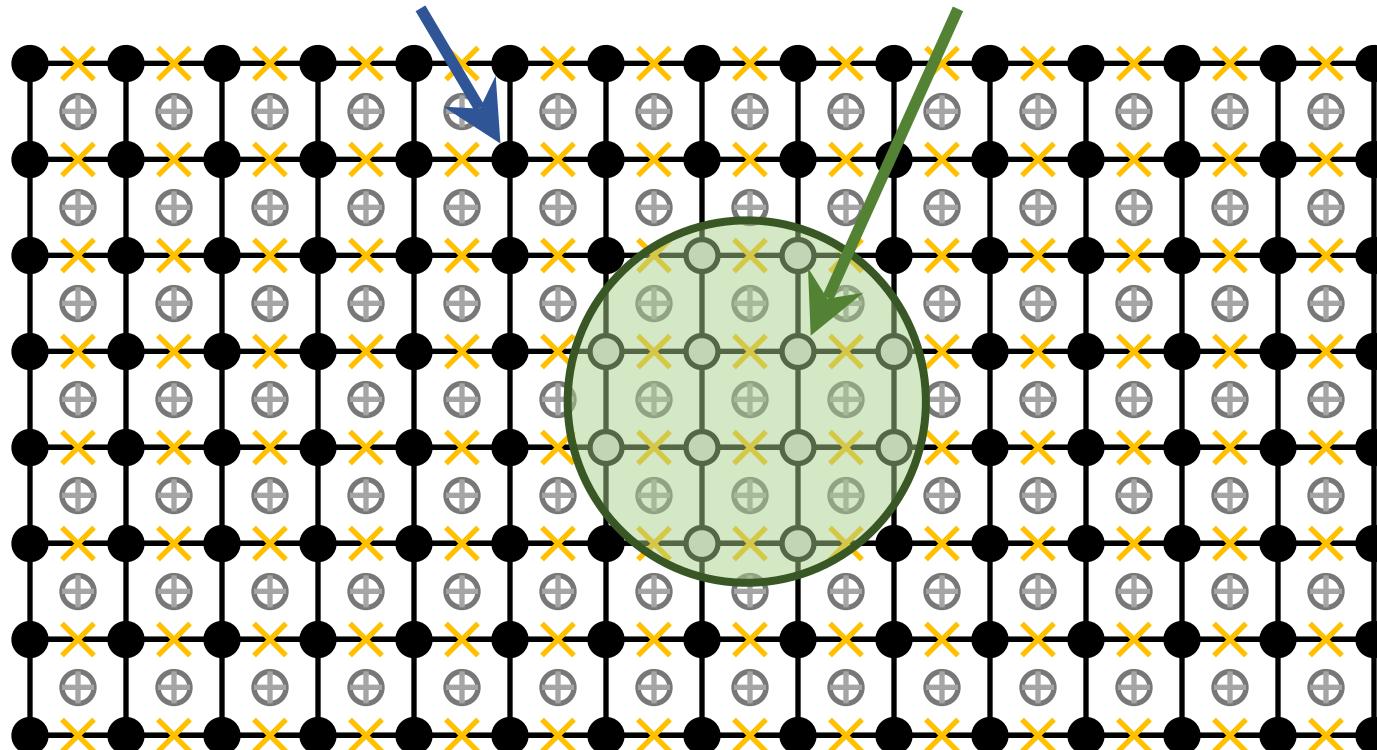
Critical current  $J_c$  (maximal possible non-dissipative current) is usually defined when voltage  $V$  is a small fraction (e.g., 1%) of the free flow value  $V_{\text{ff}}$ .



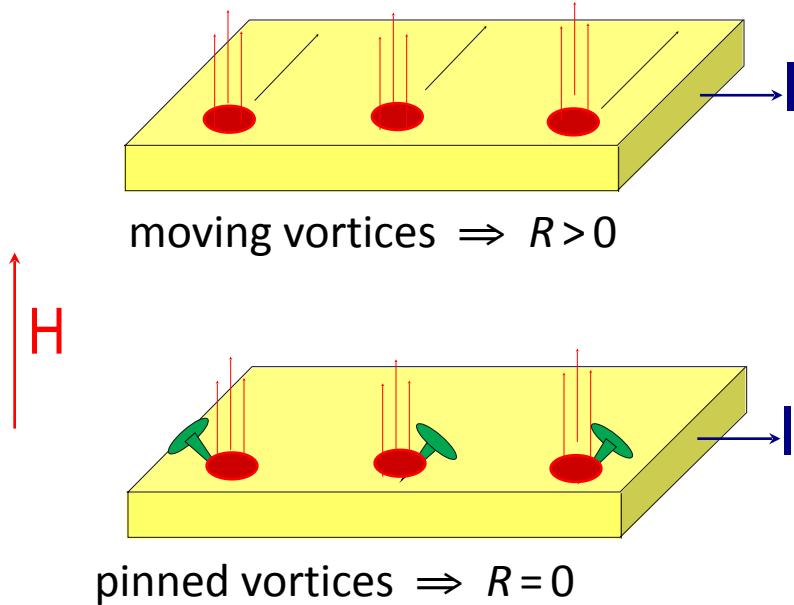
# Modelling of the inclusions

$$u(\partial_t + i\mu)\psi = \epsilon(\mathbf{r})\psi - |\psi|^2\psi + (\nabla - i\mathbf{A})^2\psi + \zeta(\mathbf{r}, t)$$

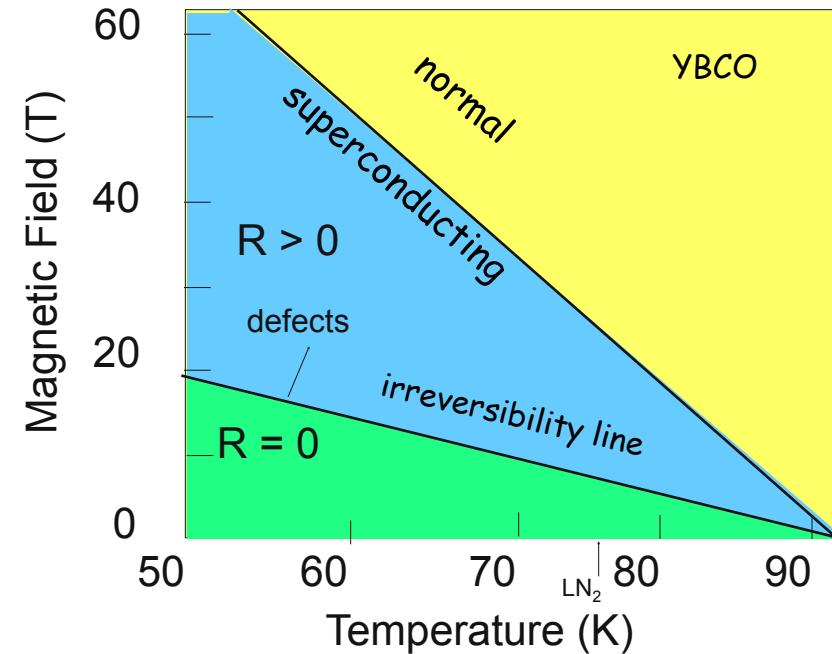
$\epsilon > 0$  in superconductor       $\epsilon < 0$  in inclusion



# Vortex motion and dissipation



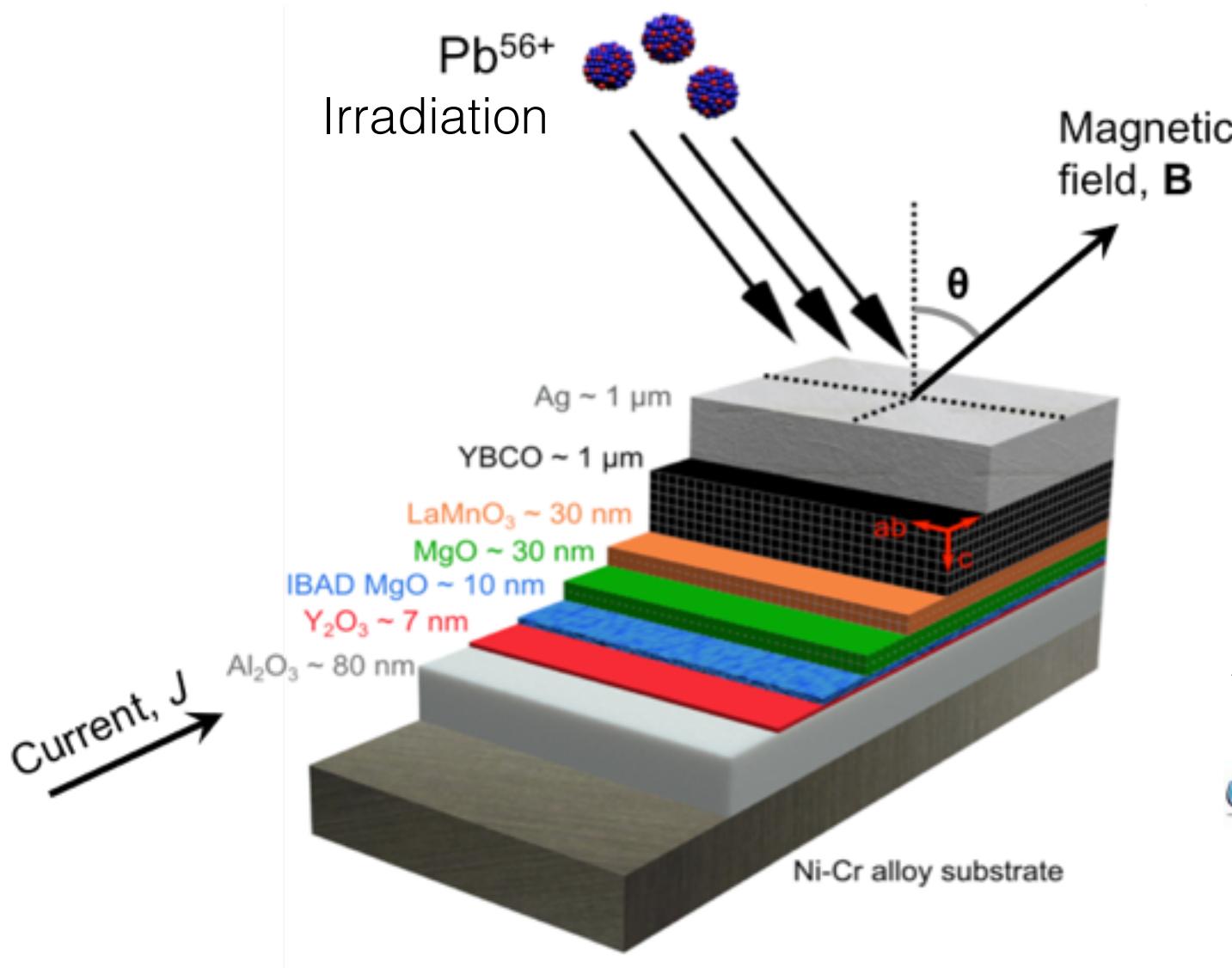
Pinning defects: nanodots,  
disorder, 2<sup>nd</sup> phases,  
dislocations, intergrowths,  
etc



Higher transition temperature  $\Rightarrow$  new materials

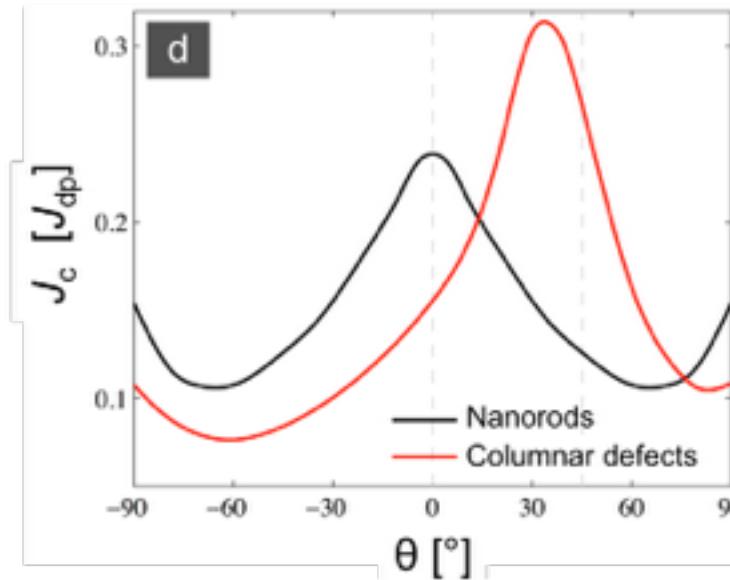
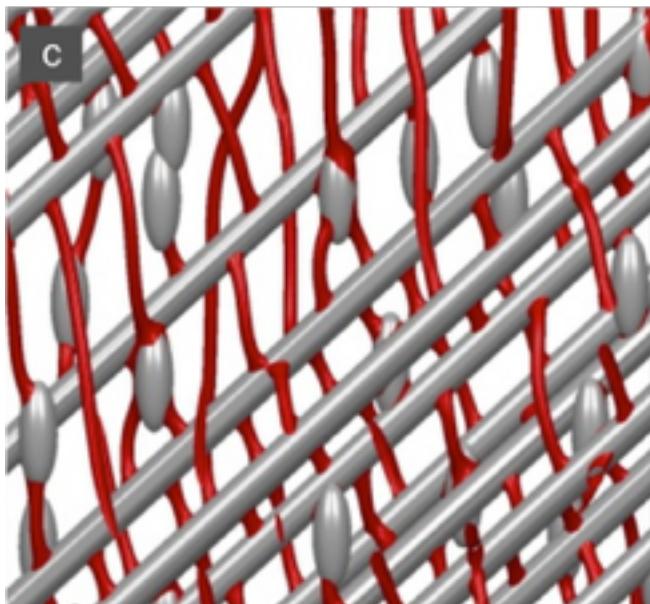
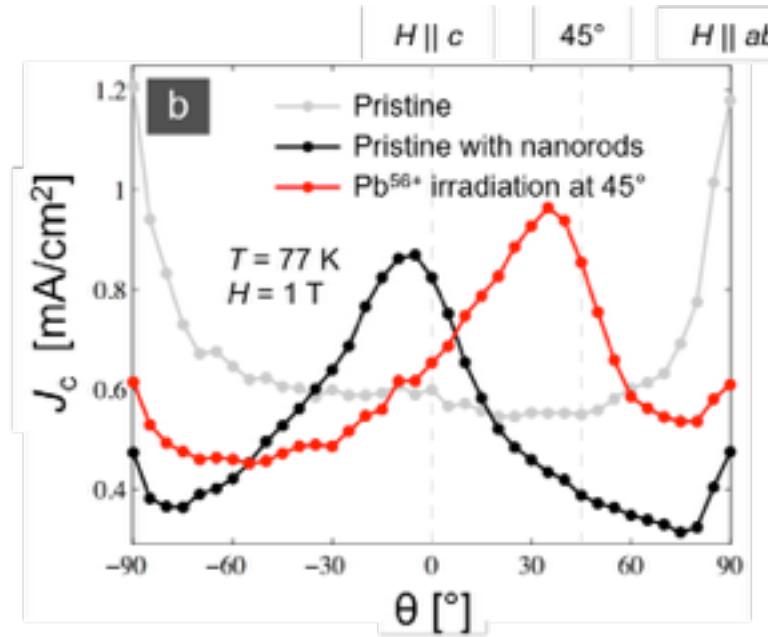
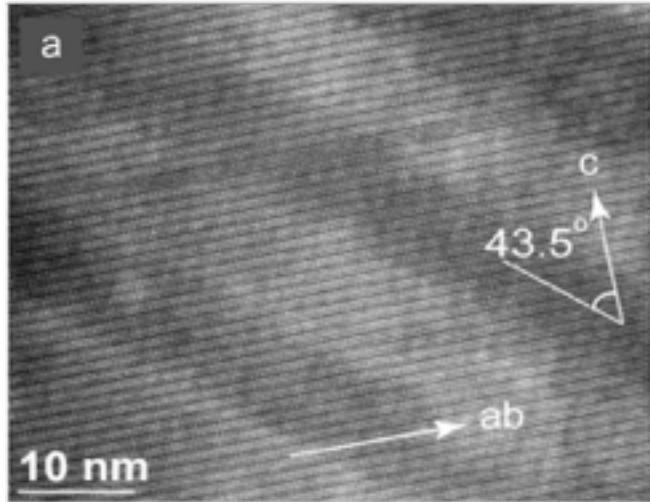
Higher currents  $\Rightarrow$  control “vortex matter”

# Materials by design



YBCO tape made by  
**SuperPower**  
Inc.  
A Furukawa Company

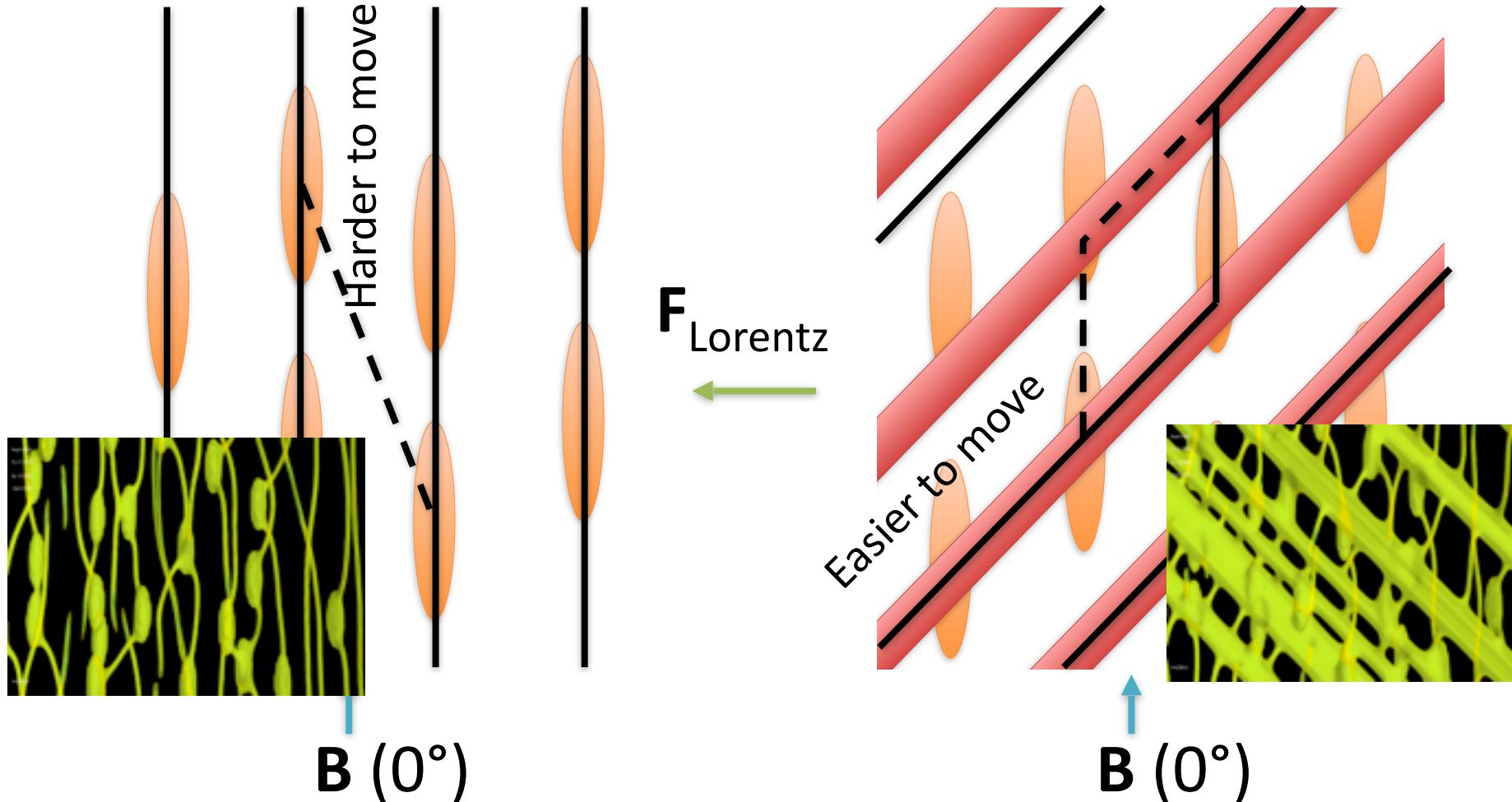
# Materials by design: Angular dependence



Experiment

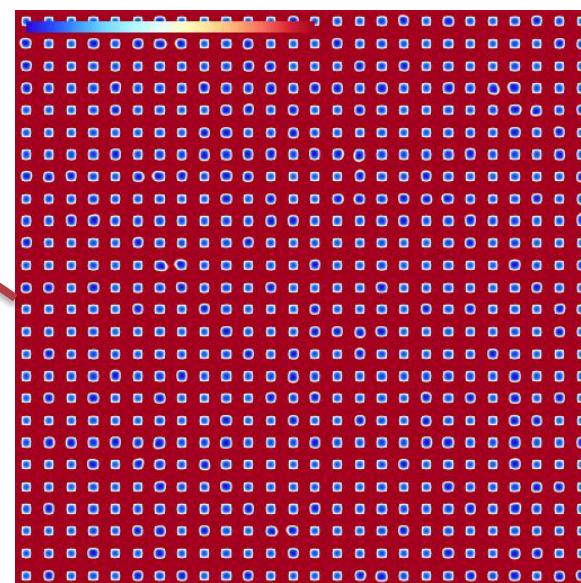
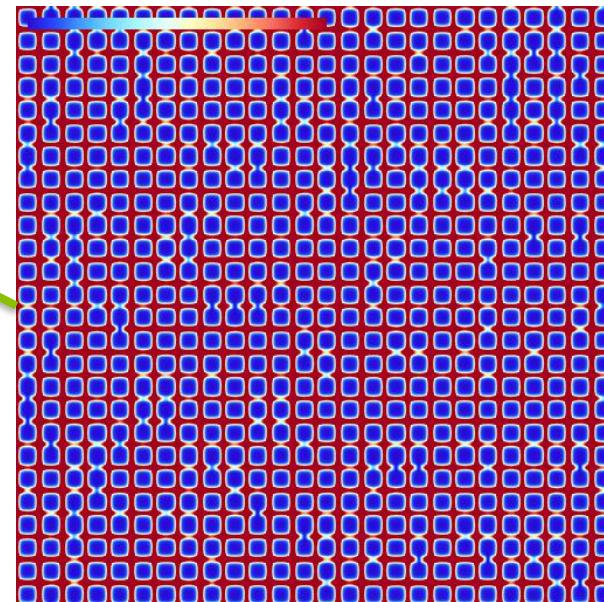
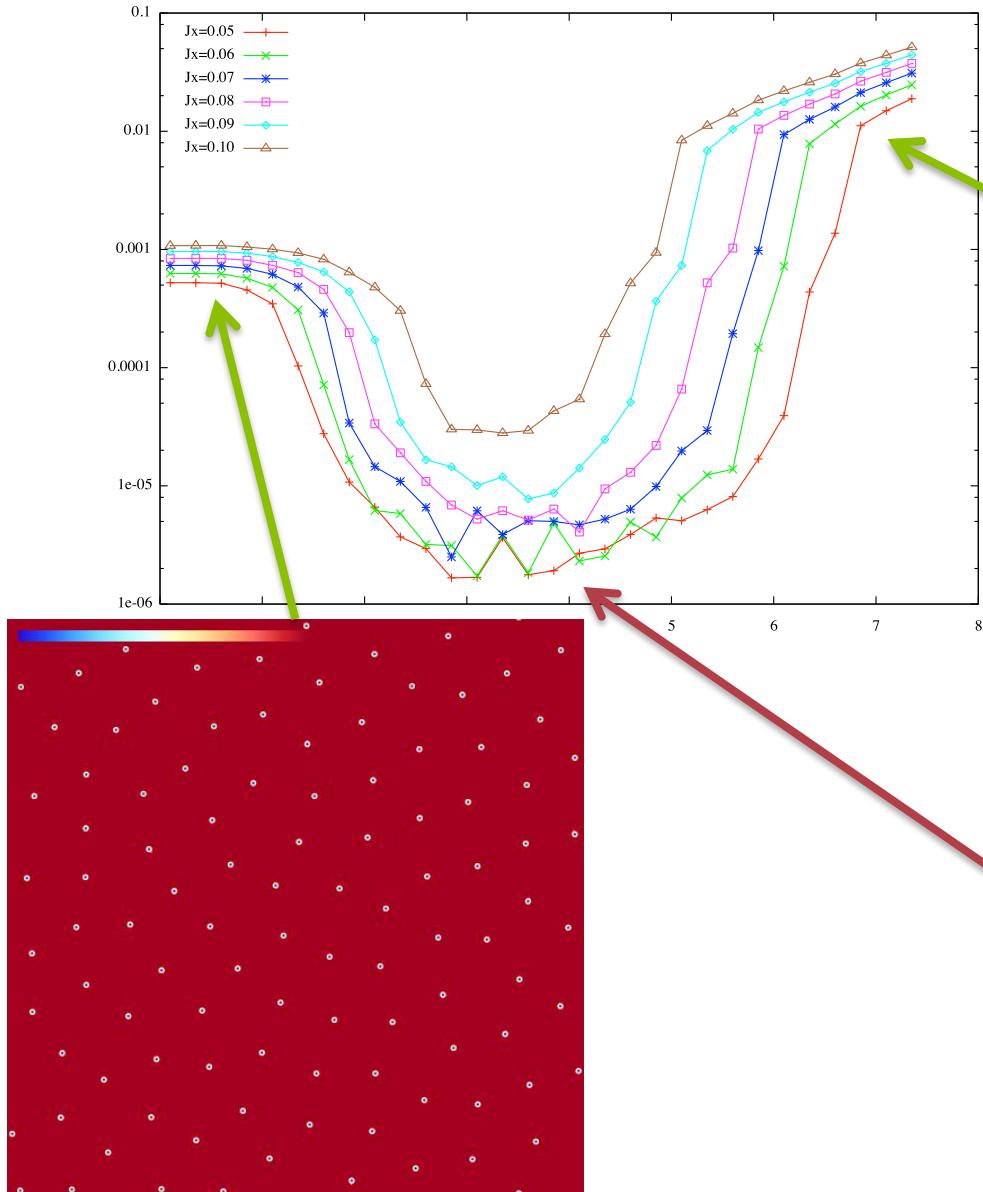
Simulations

# Materials by design: Strong non-additivity of defects



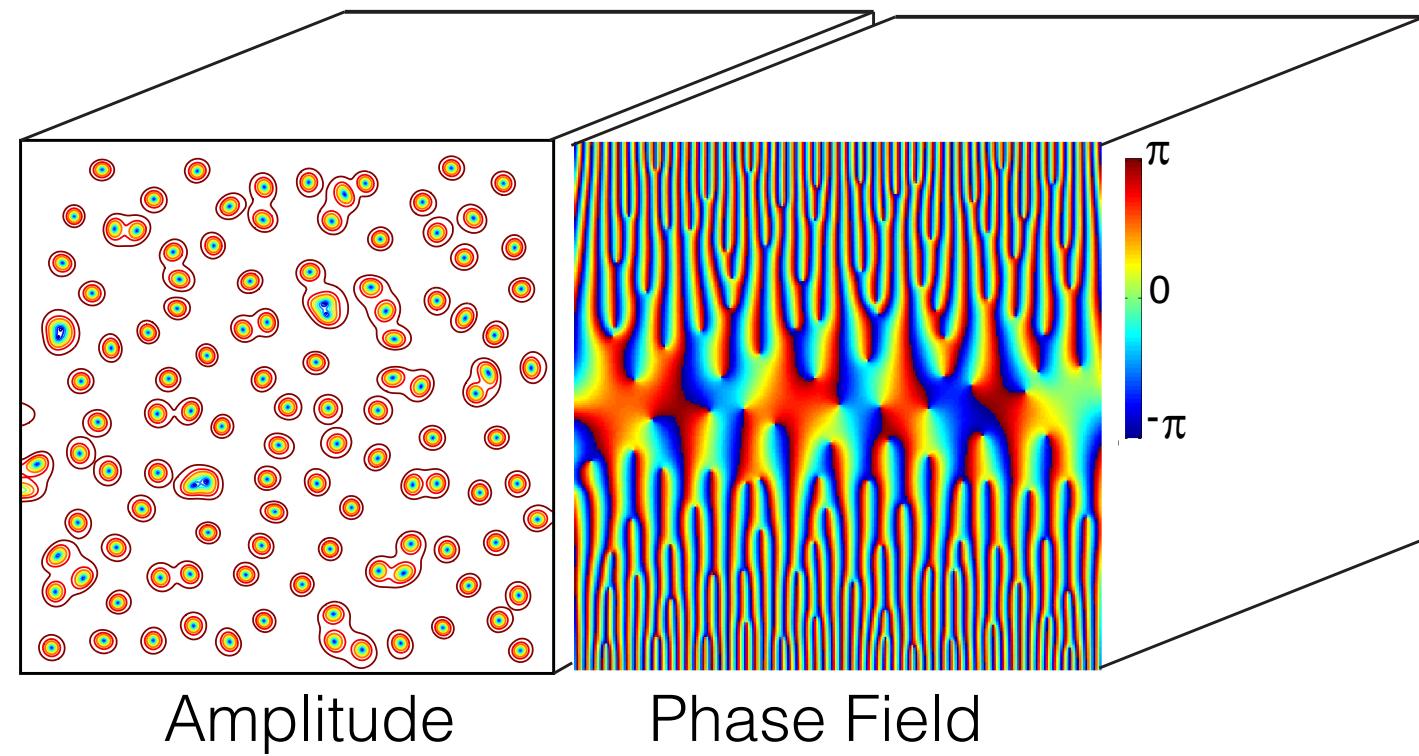
Columnar defects works like a shortcuts for magnetic vortices

# Interpreting voltage curves

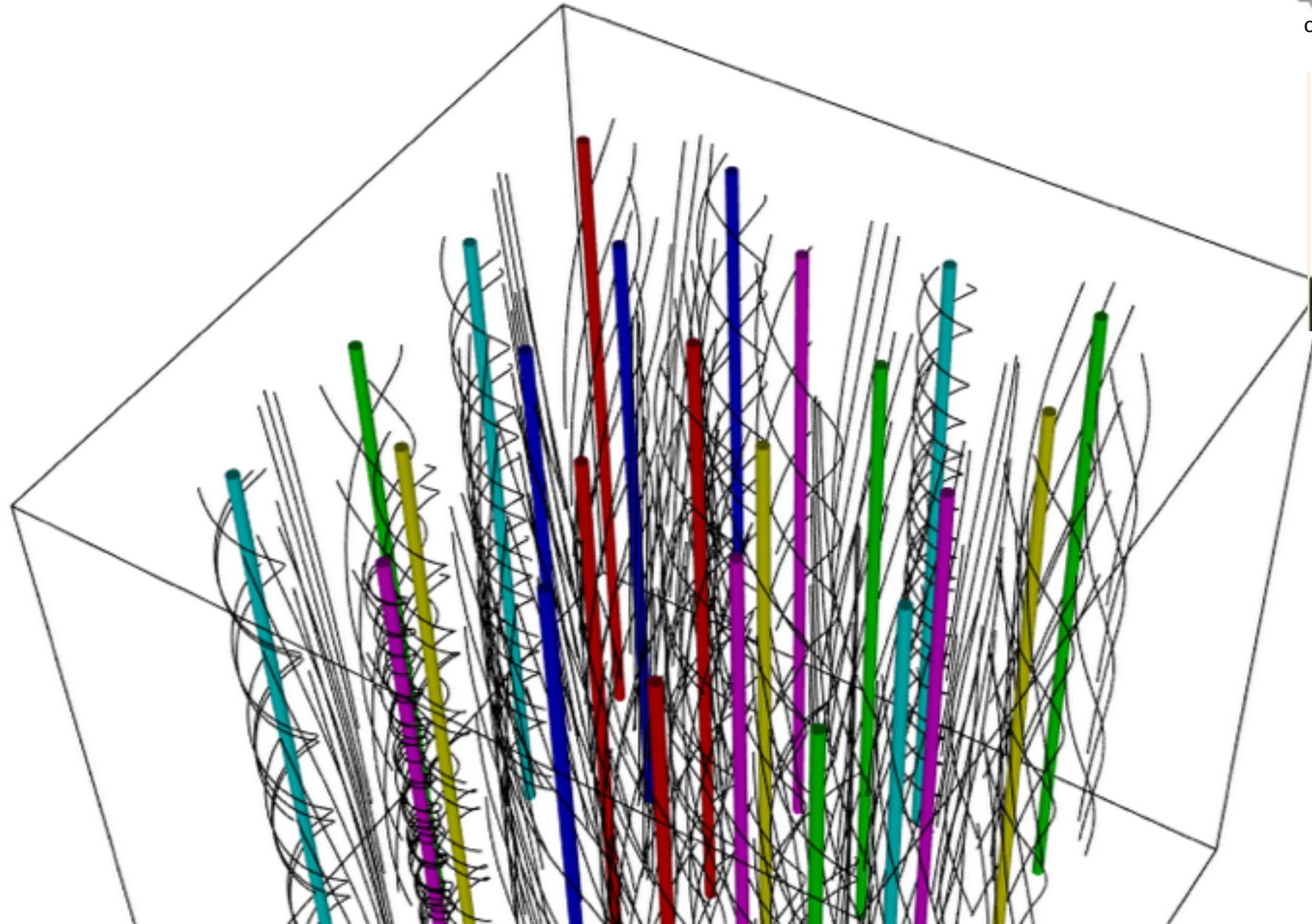


# Identifying and visualizing vortices

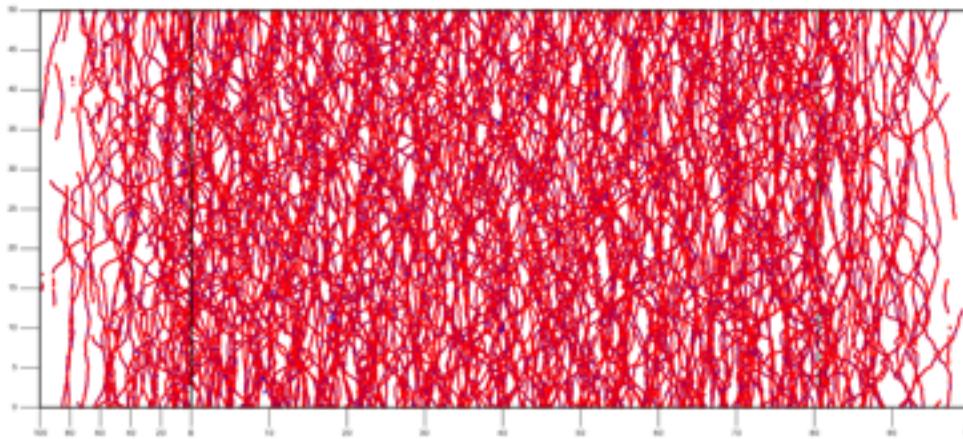
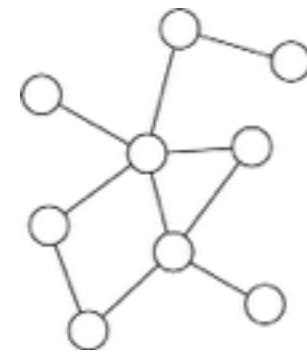
# Output of Ginzburg-Landau Simulation: complex scalar defined over mesh



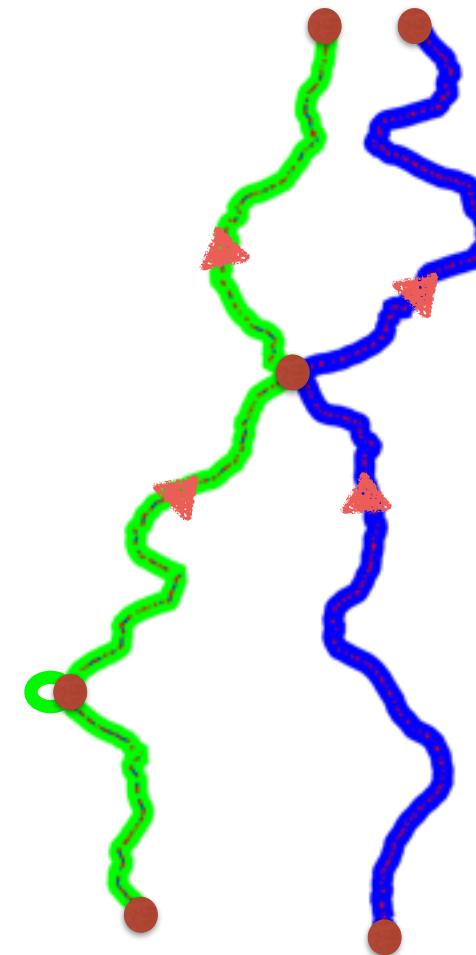
# Determining how super currents flow through the material



# Graph Analysis



- Disentangle vortices
- Remove tiny  
(unstable) loops



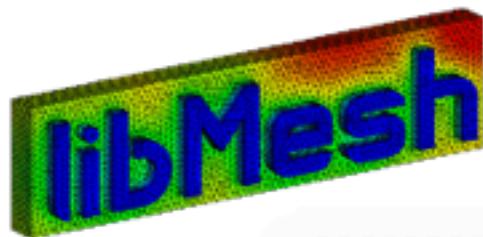
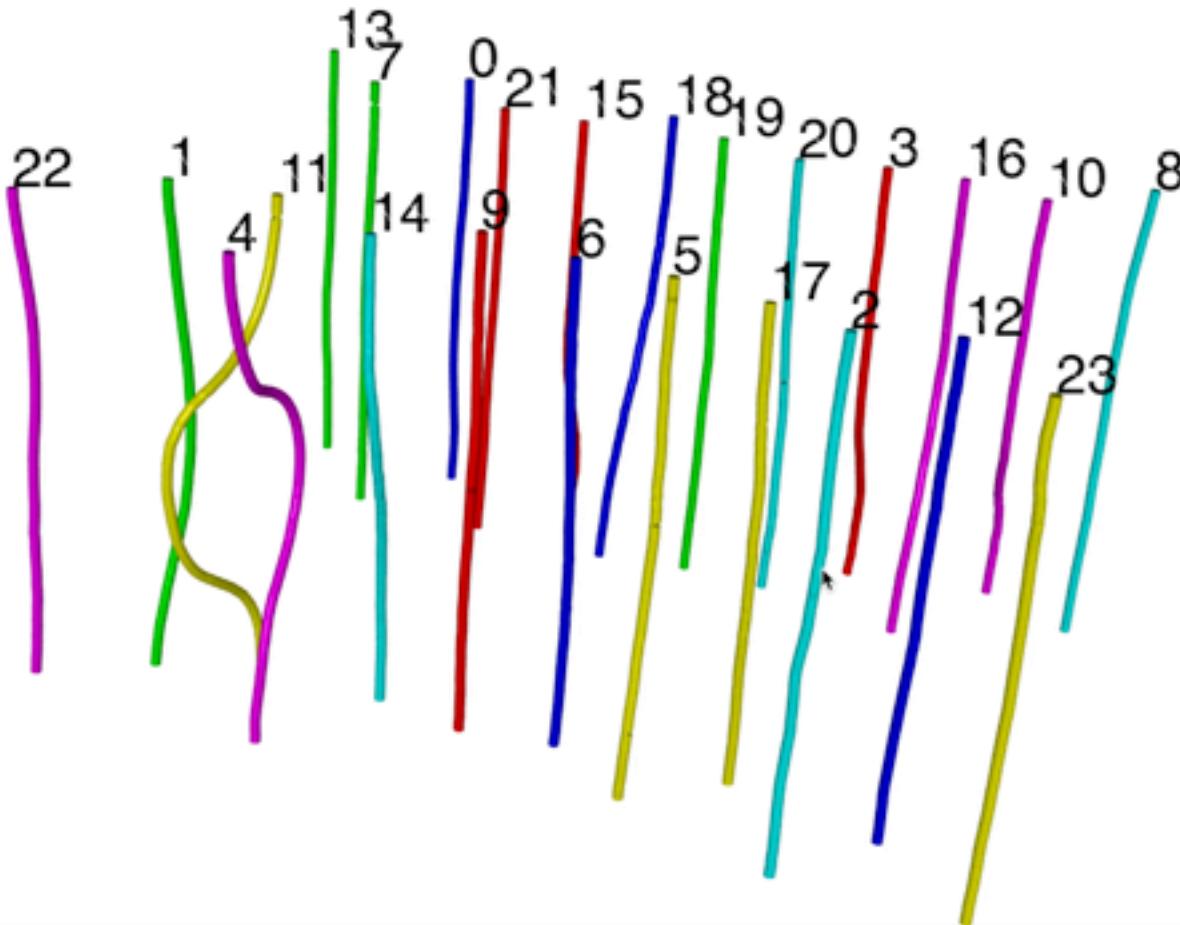
# Tracking



QuickTime Player File Edit View Window Help

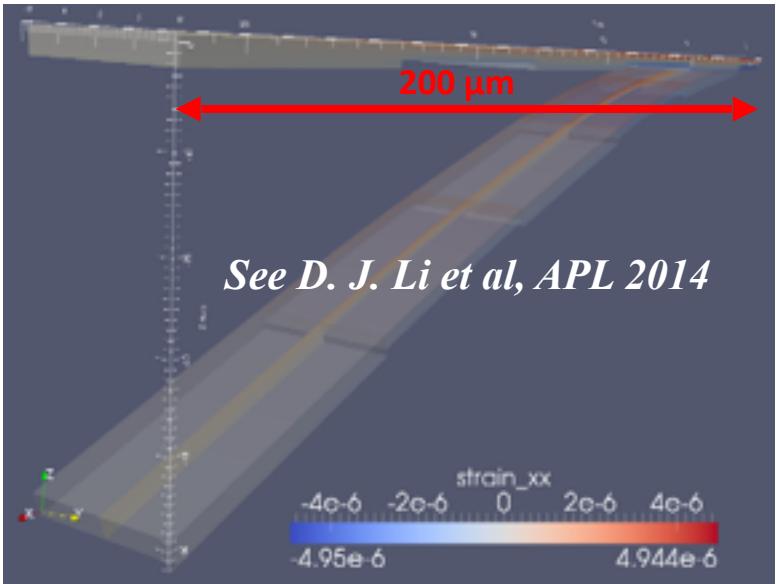
5% Sun 10:00

timestep=150

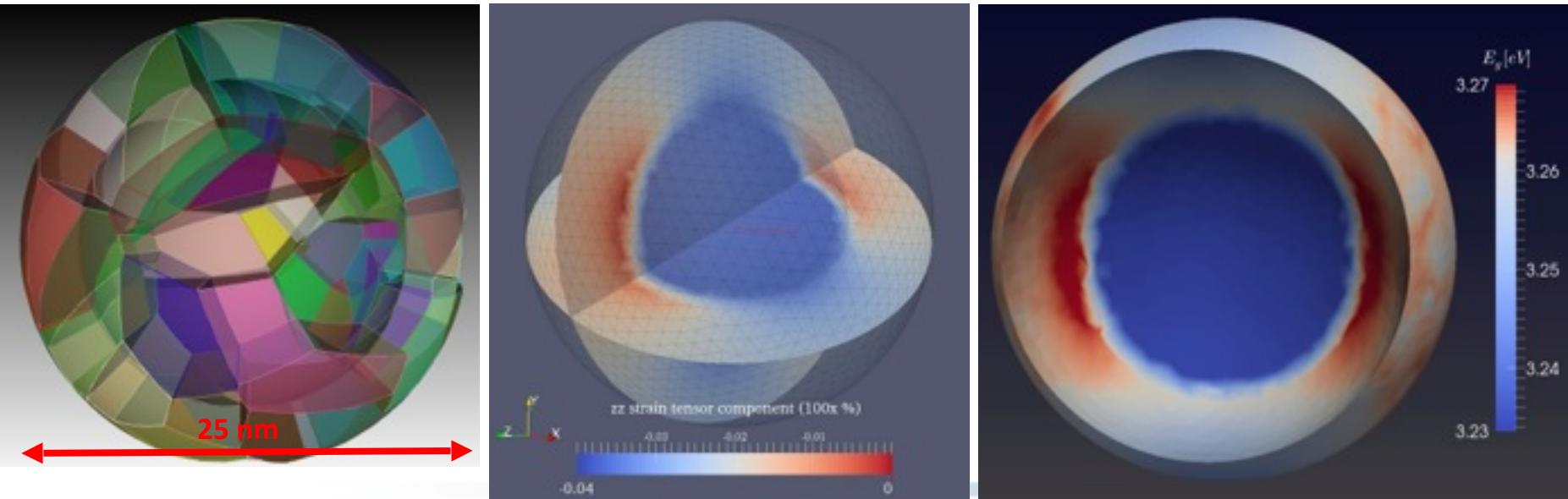


# Coupled phasefield models of solid state materials

## Energy Harvesters (with Seungbum Hong, ANL)

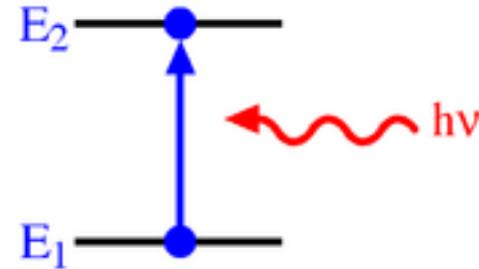
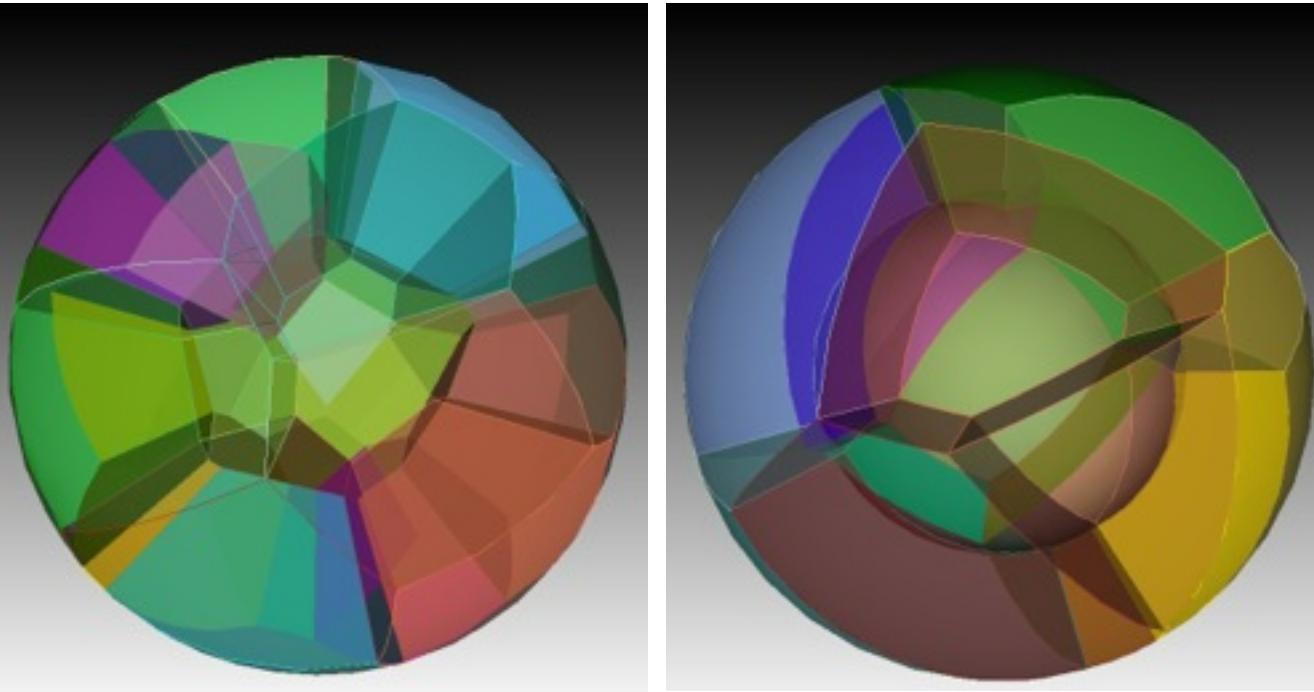


## Core-Shell Nanoparticles: from Structure to Elastic Fields to Optical Properties



# Core-Shell Nanoparticles: Structure

- Composite nanoparticles (metal-semiconductor, semiconductor-semiconductor)
- Here,  $\text{ZnO}/\text{TiO}_2$  and  $\text{Zn}/\text{ZnO}$  ~25 nm outer diameter
- Potentially useful for photovoltaics (solar absorption)

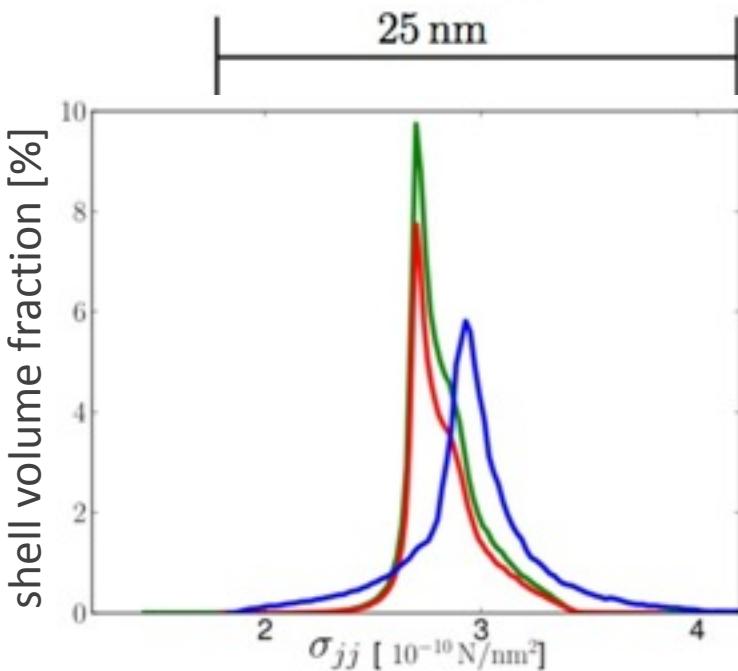
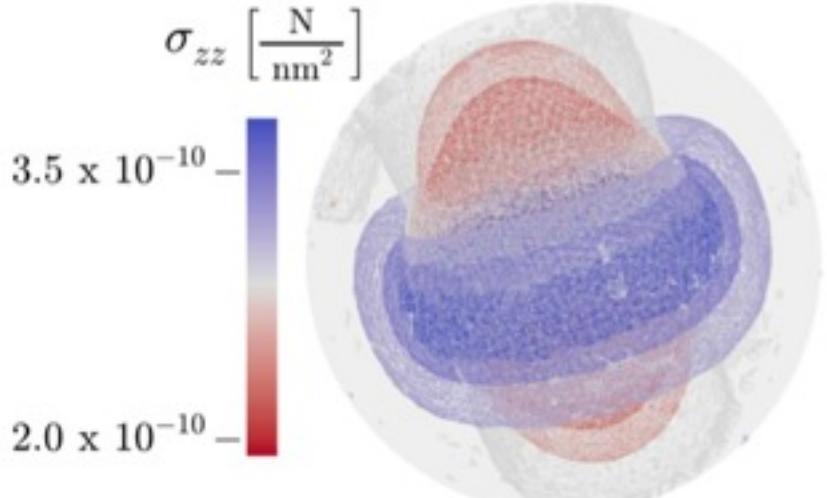


Bandgap =  $E_2 - E_1$  depends on strain

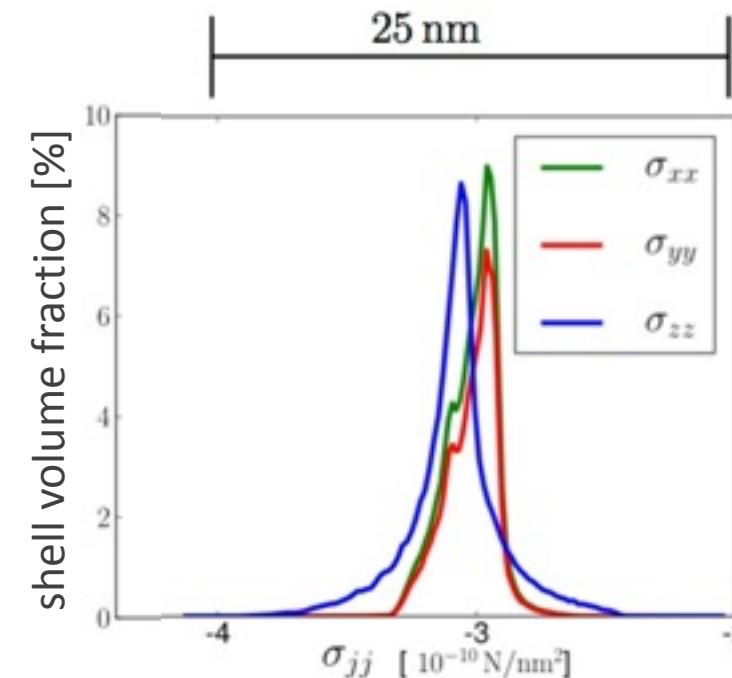
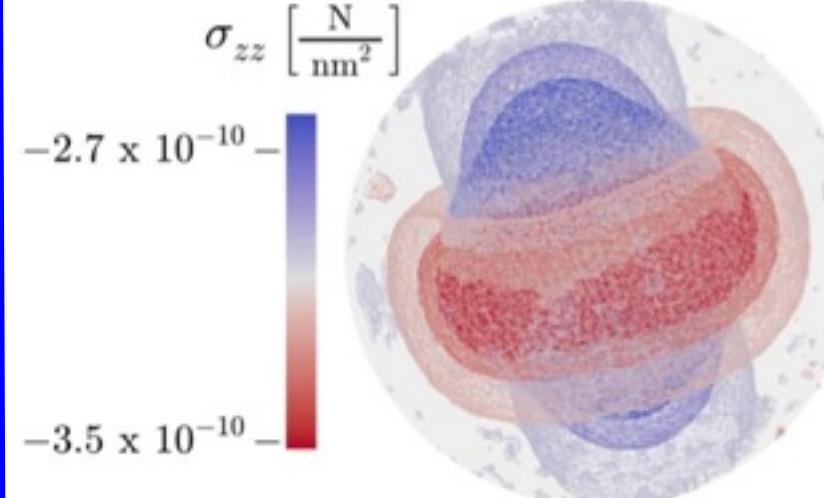
- *What is the strain/stress in a core-shell nanoparticle (bulk and surface)?*
- *How do we relate the stress to the band gap and absorption spectrum?*
- *Can we tune the absorption spectrum by tuning the stress?*

# Stress Fields in Core-Shell Nanoparticles

Spherical Zn core (hexagonal)  
Monocrystalline ZnO shell (almost isotropic)



Spherical ZnO core (almost isotropic)  
Monocrystalline TiO<sub>2</sub> shell (rutile, tetragonal)



The screenshot shows a web-based interface for managing the MOOSE framework. The URL is <https://demo.ematter.org>. The interface includes a sidebar with 'Tools' (Search tools, MATERIALS SCIENCE, MOOSE Tools, DATA TRANSFER, Globus Data Transfer, WORKFLOWS), a main panel for 'Name:' and 'Console' output, and a right-hand sidebar for 'Your History' showing task logs.

**Tools**

- Search tools
- MATERIALS SCIENCE
- MOOSE Tools
  - MOOSE
  - Ferret
- DATA TRANSFER
- Globus Data Transfer
  - Browse and Get Data via Globus Online
  - Get Data via Globus Online
  - Send Data via Globus Online
  - GO Transfer
  - Upload File
  - Directory Path Dataset
- WORKFLOWS
  - All workflows
  - Batch Submit

**Name:**

**Console:**  Output the result using the default settings for Console output.

**CSV:**  Output the scalar variable and postprocessors to a csv file using the default CSV output.

**Exodus:**  Output the results using the default settings for Exodus output.

**Interval:**  The interval at which timesteps are output to the solution file.

**Output final:**  Force the final timestep to be output, regardless of output interval.

**Output initial:**  Request that the initial condition is output to the solution file.

**Output intermediate:**  Request that all intermediate steps (not initial or final) are output.

**Types**

**About MOOSE Framework**

The Multiphysics Object-Oriented Simulation Environment (MOOSE) is a finite-element, multiphysics framework primarily developed by Idaho National Laboratory (<http://www.inl.gov>). It provides a high-level interface to some of the most sophisticated [nonlinear solver technology] (<http://www.mcs.anl.gov/petsc/>) on the planet. MOOSE presents a straight-forward API that aligns well with the real-world problems scientists and engineers need to tackle. Every detail about how an engineer interacts with MOOSE has been thought through, from the installation process through running your simulation on state-of-the-art supercomputers; the MOOSE system will accelerate your research.

Some of the capability at your fingertips:

- Fully-coupled, fully-implicit multiphysics solver
- Dimension independent physics
- Automatically parallel (front-end runs ~100,000 CPU cores)

**Your History**

ID	Task Name	Type	Status	Size	Last Modified
1	BS_SM_GCC_newton_xm_kandu.x#	ExodusII	Success	0 MB	Thu Jan 8 17:54:14 2015
2	Test0_Ferret_on_data	ExodusII	Success	708 bytes	Thu Jan 8 17:54:14 2015
3	Test0_Ferret_on_data	ExodusII	Success	0 MB	Thu Jan 8 17:54:14 2015
4	Test0_Ferret_on_data	ExodusII	Success	0 MB	Thu Jan 8 17:54:14 2015
5	Test0_Ferret_on_data	ExodusII	Success	0 MB	Thu Jan 8 17:54:14 2015
6	Test0_Ferret_on_data	ExodusII	Success	0 MB	Thu Jan 8 17:54:14 2015
7	Test0_Ferret_on_data	ExodusII	Success	0 MB	Thu Jan 8 17:54:14 2015
8	Test0_Ferret_on_data	ExodusII	Success	0 MB	Thu Jan 8 17:54:14 2015
9	mug.e	ExodusII	Success	0 MB	Thu Jan 8 17:54:14 2015

- Hides software stack
- Multiple hardware resources
  - Amazon
  - Remote clusters
  - *Mira*
  - *GPU clusters*
- Integrate multiple tools
  - Workflows
  - Batch runs
  - Parameter sweeps
  - Sensitivity/UQ
  - Postprocessing
  - Visualization
- Data management
  - Archive
  - Share
  - Publish
- Focus on configuration of kernels into a usable app