

PETSc Tutorial

PETSc Team
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AMCS E4302
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This PETSc Tutorial debuts Tonight!



Enable students to develop new simulations with PETSc.

- Serial and Parallel

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- Linear and Nonlinear

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- Finite Difference and Finite Element

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- Optimal Solvers

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Items in red not finished for tutorial

- ① A Minimal PETSc Application
- ② Creating a Simple 2D Mesh
- ③ Mesh Functions
- ④ Mesh Operators
- ⑤ Systems of Equations
- ⑥ Higher Dimensions
- ⑦ Unfinished Business

Part I

Creating a PETSc Application

PETSc was developed as a Platform for Experimentation

We want to experiment with different

- Models
- Discretizations
- Solvers
- Algorithms (which blur these boundaries)

What I Need From You

- Tell me if you do not understand
- Tell me if an example does not work
- Suggest better wording or **figures**
- Followup problems at petsc-maint@mcs.anl.gov

How Can We Help?

- Provide documentation
- Answer email at petsc-maint@mcs.anl.gov

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- Provide documentation
- Quickly answer questions
- Help install
- Guide large scale flexible code development
- Answer email at petsc-maint@mcs.anl.gov

The Role of PETSc

Developing parallel, nontrivial PDE solvers that deliver high performance is still difficult and requires months (or even years) of concentrated effort.

*PETSc is a toolkit that can ease these difficulties and reduce the development time, but it is not a black-box PDE solver, nor a **silver bullet**.*

What is PETSc?

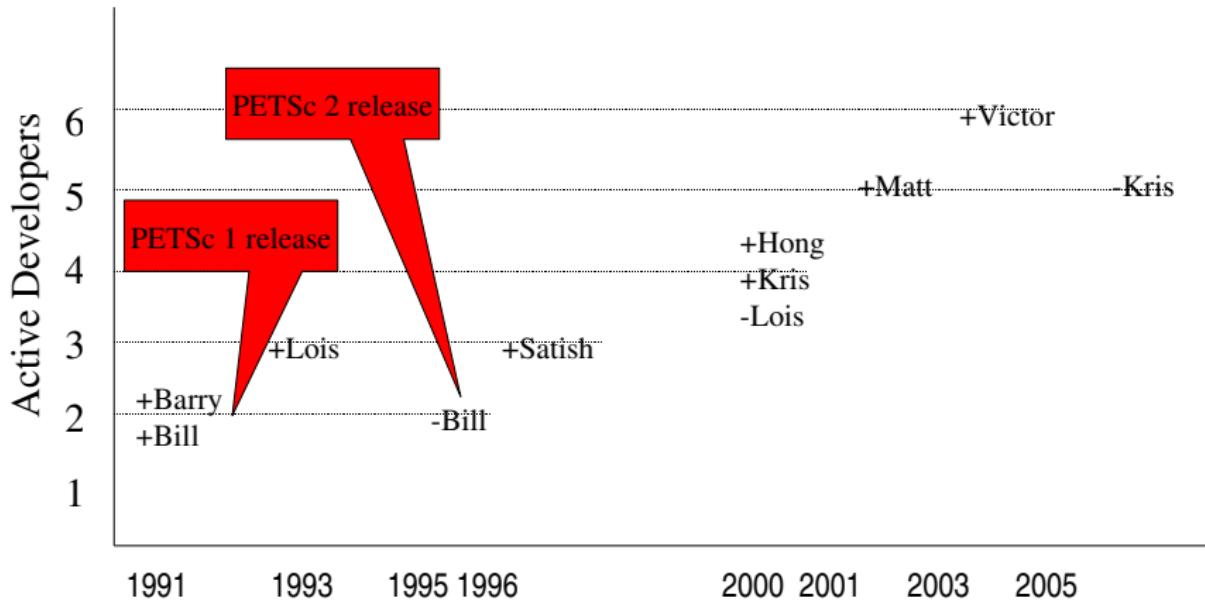
A freely available and supported research code

- Download from <http://www.mcs.anl.gov/petsc>
- Free for everyone, including industrial users
- Hyperlinked manual, examples, and manual pages for all routines
- Hundreds of tutorial-style examples
- Support via email: petsc-maint@mcs.anl.gov
- Usable from C, C++, Fortran 77/90, and Python

What is PETSc?

- Portable to any parallel system supporting MPI, including:
 - Tightly coupled systems
 - Cray T3E, SGI Origin, IBM SP, HP 9000, Sub Enterprise
 - Loosely coupled systems, such as networks of workstations
 - Compaq, HP, IBM, SGI, Sun, PCs running Linux or Windows
- PETSc History
 - Begun September 1991
 - Over 8,500 downloads since 1995 (version 2), currently 250 per month
- PETSc Funding and Support
 - Department of Energy
 - SciDAC, MICS Program
 - National Science Foundation
 - CIG, CISE, Multidisciplinary Challenge Program

Timeline



What Can We Handle?

- PETSc has run problems with over **500 million** unknowns
 - <http://www.scconference.org/sc2004/schedule/pdfs/pap111.pdf>

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 - ftp://info.mcs.anl.gov/pub/tech_reports/reports/P776.ps.Z

What Can We Handle?

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- PETSc has run on over **6,000** processors efficiently
 - ftp://info.mcs.anl.gov/pub/tech_reports/reports/P776.ps.Z
- PETSc applications have run at **2 Teraflops**
 - LANL PFLOTRAN code

Who Uses PETSc?

- Computational Scientists
 - PyLith (TECTON), Underworld, Columbia group
- Algorithm Developers
 - Iterative methods and Preconditioning researchers
- Package Developers
 - SLEPc, TAO, MagPar, StGermain, DealII

The PETSc Team



Bill Gropp



Barry Smith



Satish Balay



Dinesh Kaushik



Kris Buschelman



Matt Knepley



Hong Zhang



Victor Eijkhout



Lois McInnes

Downloading PETSc

- The latest tarball is on the PETSc site
 - <ftp://ftp.mcs.anl.gov/pub/petsc/petsc.tar.gz>
 - We no longer distribute patches (everything is in the distribution)
- There is a Debian package
- There is a FreeBSD Port
- There is a Mercurial development repository

Cloning PETSc

- The full development repository is open to the public
 - <http://mercurial.mcs.anl.gov/petsc/petsc-dev>
 - <http://mercurial.mcs.anl.gov/petsc/BuildSystem>
- Why is this better?
 - You can clone to any release (or any specific ChangeSet)
 - You can easily rollback changes (or releases)
 - You can get fixes from us the same day

Unpacking PETSc

- Just clone development repository
 - `hg clone http://mercurial.mcs.anl.gov/petsc/petsc-dev petsc-dev`
 - `hg clone -rRelease-2.3.1 petsc-dev petsc-2.3.1`

or

- Unpack the tarball
 - `tar xzf petsc.tar.gz`

Getting the Source

You will need the Developer copy of PETSc:

- Using Mercurial

```
hg clone http://mercurial.mcs.anl.gov/petsc/petsc-dev  
cd petsc-dev/python  
hg clone http://mercurial.mcs.anl.gov/petsc/BuildSystem
```

- Manual download

```
wget ftp://info.mcs.anl.gov/pub/petsc/petsc-dev.tar.gz .
```

and the tutorial source code:

- Using Mercurial

```
hg clone http://mercurial.mcs.anl.gov/petsc/Columbia06TutorialCode
```

- Manual download

```
wget ftp://info.mcs.anl.gov/pub/petsc/Columbia06TutorialCode.tar.gz .
```

Configuring PETSc

- Set \$PETSC_DIR to the installation root directory
- Run the configuration utility
 - \$PETSC_DIR/config/configure.py
 - \$PETSC_DIR/config/configure.py --help
 - \$PETSC_DIR/config/configure.py --download-mpich
- There are many examples on the installation page
- Configuration files are placed in \$PETSC_DIR/bmake/\$PETSC_ARCH
 - \$PETSC_ARCH has a default if not specified

Configuring PETSc

- You can easily reconfigure with the same options
 - `./bmake/$PETSC_ARCH/configure.py`
- Can maintain several different configurations
 - `./config/configure.py -PETSC_ARCH=linux-fast --with-debugging=0`
- All configuration information is in `configure.log`
 - ALWAYS send this file with bug reports

Automatic Downloads

- Starting in 2.2.1, some packages are automatically
 - Downloaded
 - Configured and Built (in \$PETSC_DIR/externalpackages)
 - Installed in PETSc
- Currently works for
 - PETSc documentation utilities (Sowing, Igrend, c2html)
 - BLAS, LAPACK, BLACS, ScaLAPACK, PLAPACK
 - MPICH, MPE, LAM
 - ParMetis, Chaco, Jostle, Party, Scotch
 - MUMPS, Spooles, SuperLU, SuperLU_Dist, UMFPack
 - Prometheus, HYPRE, ML, SPAI
 - Sundials
 - Triangle, TetGen
 - FIAT, FFC

Building PETSc

- Uses recursive make starting in `cd $PETSC_DIR`
 - `make`
 - Check build when done with `make test`
- Complete log for each build in `make_log-$PETSC_ARCH`
 - ALWAYS send this with bug reports
- Can build multiple configurations
 - `PETSC_ARCH=linux-fast make`
 - Libraries are in `$PETSC_DIR/lib/$PETSC_ARCH/`
- Can also build a subtree
 - `cd src/snss; make`
 - `cd src/snss; make ACTION=libfast tree`

Running PETSc

- Try running PETSc examples first
 - `cd $PETSC_DIR/src/snes/examples/tutorials`
- Build examples using make targets
 - `make ex5`
- Run examples using the make target
 - `make runex5`
- Can also run using MPI directly
 - `mpirun ./ex5 -snes_max_it 5`
 - `mpiexec ./ex5 -snes_monitor`

Using MPI

- The Message Passing Interface is:
 - a library for parallel communication
 - a system for launching parallel jobs (mpirun/mpiexec)
 - a community standard
- Launching jobs is easy
 - `mpiexec -np 4 ./ex5`
- You should never have to make MPI calls when using PETSc
 - Almost never

MPI Concepts

- Communicator
 - A context (or scope) for parallel communication ("Who can I talk to")
 - There are two defaults:
 - yourself (PETSC_COMM_SELF),
 - and everyone launched (PETSC_COMM_WORLD)
 - Can create new communicators by splitting existing ones
 - Every PETSc object has a communicator
- Point-to-point communication
 - Happens between two processes (like in MatMult())
- Reduction or scan operations
 - Happens among all processes (like in VecDot())

Alternative Memory Models

- Single process (address space) model
 - OpenMP and threads in general
 - Fortran 90/95 and compiler-discovered parallelism
 - System manages memory and (usually) thread scheduling
 - Named variables refer to the same storage
- Single name space model
 - HPF, UPC
 - Global Arrays
 - Titanium
 - Named variables refer to the coherent values (distribution is automatic)
- Distributed memory (shared nothing)
 - Message passing
 - Names variables in different processes are unrelated

Common Viewing Options

- Gives a text representation
 - `-vec_view`
- Generally views subobjects too
 - `-snes_view`
- Can visualize some objects
 - `-mat_view_draw`
- Alternative formats
 - `-vec_view_binary`, `-vec_view_matlab`, `-vec_view_socket`
- Sometimes provides extra information
 - `-mat_view_info`, `-mat_view_info_detailed`

Common Monitoring Options

- Display the residual
 - `-ksp_monitor`, graphically `-ksp_xmonitor`
- Can disable dynamically
 - `-ksp_cancelmonitors`
- Does not display subsolvers
 - `-snes_monitor`
- Can use the true residual
 - `-ksp_truemonitor`
- Can display different subobjects
 - `-snes_vecmonitor`, `-snes_vecmonitor_update`,
`-snes_vecmonitor_residual`
 - `-ksp_gmres_krylov_monitor`
- Can display the spectrum
 - `-ksp_singmonitor`

Getting More Help

- <http://www.mcs.anl.gov/petsc>
- Hyperlinked documentation
 - Manual
 - Manual pages for every method
 - HTML of all example code (linked to manual pages)
- FAQ
- Full support at petsc-maint@mcs.anl.gov
- High profile users
 - David Keyes
 - Rich Martineau
 - Richard Katz
 - Charles Williams

Following the Tutorial

Update to each new checkpoint (**r0**):

- hg clone -r0 Columbia06TutorialCode code-test

or

- hg update 0

Build the executable with `make`, and then run:

- make runbratu
- make debugbratu
- make valbratu
- make NP=2 runbratu
- make EXTRA_ARGS="-pc_type jacobi" runbratu

Code Update

Update to Revision 0

Initialization

- Call `PetscInitialize()`
 - Setup static data and services
 - Setup MPI if it is not already
- Call `PetscFinalize()`
 - Calculates logging summary
 - Shutdown and release resources
- Checks compile and link

Command Line Processing

- Check for an option
 - `PetscOptionsHasName()`
- Retrieve a value
 - `PetscOptionsGetInt()`, `PetscOptionsGetIntArray()`
- Set a value
 - `PetscOptionsSetValue()`
- Clear, alias, reject, etc.

Profiling

- Use `-log_summary` for a performance profile
 - Event timing
 - Event flops
 - Memory usage
 - MPI messages
- Call `PetscLogStagePush()` and `PetscLogStagePop()`
 - User can add new stages
- Call `PetscLogEventBegin()` and `PetscLogEventEnd()`
 - User can add new events

Part II

Creating a Simple 2D Mesh

Higher Level Abstractions

The PETSc DA class is a topology and discretization interface.

- Structured grid interface
 - Fixed simple topology
- Supports stencils, communication, reordering
 - Limited idea of operators
- Nice for simple finite differences

The PETSc Mesh class is a topology interface.

- Unstructured grid interface
 - Arbitrary topology and element shape
- Supports partitioning, distribution, and global orders

Higher Level Abstractions

The PETSc DM class is a hierarchy interface.

- Supports multigrid
 - DMMG combines it with the MG preconditioner
- Abstracts the logic of multilevel methods

The PETSc Section class is a function interface.

- Functions over unstructured grids
 - Arbitrary layout of degrees of freedom
- Support distribution and assembly

Code Update

Update to Revision 2

Creating a DA

```
DACreate2d(comm, wrap, type, M, N, m, n, dof, s, lm[],  
ln[], DA *da)
```

wrap: Specifies periodicity

- DA_NONPERIODIC, DA_XPERIODIC, DA_YPERIODIC, or DA_XYPERIODIC

type: Specifies stencil

- DA_STENCIL_BOX or DA_STENCIL_STAR

M/N: Number of grid points in x/y-direction

m/n: Number of processes in x/y-direction

dof: Degrees of freedom per node

s: The stencil width

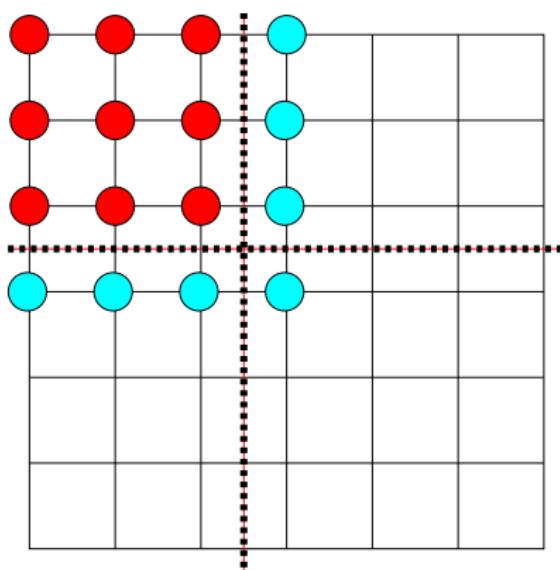
lm/n: Alternative array of local sizes

- Use PETSC_NULL for the default

Ghost Values

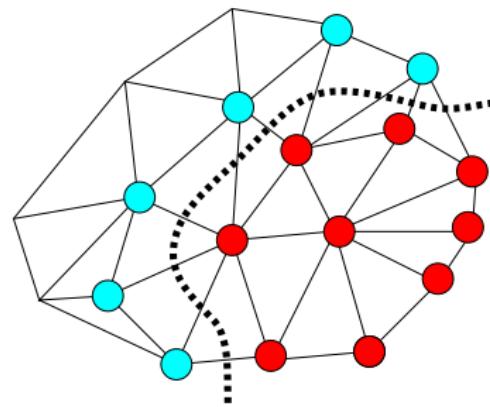
To evaluate a local function $f(x)$, each process requires

- its local portion of the vector x
- its **ghost values**, bordering portions of x owned by neighboring processes



Local Node

Ghost Node



DA Global Numberings

Proc 2			Proc 3	
Proc 0	Proc 1		Proc 0	Proc 1
25	26	27	28	29
20	21	22	23	24
15	16	17	18	19
10	11	12	13	14
5	6	7	8	9
0	1	2	3	4

Natural numbering

Proc 2			Proc 3	
Proc 0	Proc 1		Proc 0	Proc 1
21	22	23	28	29
18	19	20	26	27
15	16	17	24	25
6	7	8	13	14
3	4	5	11	12
0	1	2	9	10

PETSc numbering

DA Global vs. Local Numbering

- **Global:** Each vertex belongs to a unique process and has a unique id
- **Local:** Numbering includes **ghost** vertices from neighboring processes

Proc 2			Proc 3	
X	X	X	X	X
X	X	X	X	X
12	13	14	15	X
8	9	10	11	X
4	5	6	7	X
0	1	2	3	X
Proc 0		Proc 1		

Local numbering

Proc 2			Proc 3	
21	22	23	28	29
18	19	20	26	27
15	16	17	24	25
6	7	8	13	14
3	4	5	11	12
0	1	2	9	10
Proc 0		Proc 1		

Global numbering

Viewing the DA

- `make NP=1 EXTRA_ARGS="-da_view_draw -draw_pause -1" runbratu`
- `make NP=1 EXTRA_ARGS="-da_grid_x 10 -da_grid_y 10 -da_view_draw -draw_pause -1" runbratu`
- `make NP=4 EXTRA_ARGS="-da_grid_x 10 -da_grid_y 10 -da_view_draw -draw_pause -1" runbratu`

Correctness Debugging

- Automatic generation of tracebacks
- Detecting memory corruption and leaks
- Optional user-defined error handlers

Interacting with the Debugger

- Launch the debugger
 - `-start_in_debugger [gdb, dbx, noxterm]`
 - `-on_error_attach_debugger [gdb, dbx, noxterm]`
- Attach the debugger only to some parallel processes
 - `-debugger_nodes 0,1`
- Set the display (often necessary on a cluster)
 - `-display khan.mcs.anl.gov:0.0`

Debugging Tips

- Putting a breakpoint in `PetscError()` can catch errors as they occur
- PETSc tracks memory overwrites at the beginning and end of arrays
 - The `CHKMEMQ` macro causes a check of all allocated memory
 - Track memory overwrites by bracketing them with `CHKMEMQ`
- PETSc checks for leaked memory
 - Use `PetscMalloc()` and `PetscFree()` for all allocation
 - Option `-trmalloc` will print unfreed memory on `PetscFinalize()`

Memory Debugging

We can check for unfreed memory using:

```
make EXTRA_ARGS="-malloc_dump" runbratu
```

All options can be seen using:

```
make EXTRA_ARGS="-help" runbratu
```

Code Update

Update to Revision 3

Creating the Mesh

- File input
 - `MeshCreatePCICE()`
 - `MeshCreatePyLith()`
- Generation
 - `ALE::Generator::generateMesh()`
 - `ALE::Generator::refineMesh()`
- Partitioning and Distribution
 - `MeshDistribute()`

Code Update

Update to Revision 4

Viewing the Mesh

- `make NP=1 EXTRA_ARGS="-structured 0 -mesh_view_vtk" runbratu`
- `mayavi -d bratu.vtk -m SurfaceMap&`
- `make NP=4 EXTRA_ARGS="-structured 0 -mesh_view_vtk" runbratu`
- Viewable using Mayavi

Part III

Defining a Function

A DA is more than a Mesh

A DA contains **topology**, **geometry**, and an implicit Q1 **discretization**.

It is used as a template to create

- Vectors (functions)
- Matrices (linear operators)

DA Vectors

- The DA object contains only layout (topology) information
 - All field data is contained in PETSc Vecs
- Global vectors are parallel
 - Each process stores a unique local portion
 - `DACreateGlobalVector(DA da, Vec *gvec)`
- Local vectors are sequential (and usually temporary)
 - Each process stores its local portion plus ghost values
 - `DACreateLocalVector(DA da, Vec *lvec)`
 - includes ghost values!

Updating Ghosts

Two-step process enables overlapping computation and communication

- `DAGlobalToLocalBegin(da, gvec, mode, lvec)`
 - `gvec` provides the data
 - `mode` is either `INSERT_VALUES` or `ADD_VALUES`
 - `lvec` holds the local and ghost values
- `DAGlobalToLocal End(da, gvec, mode, lvec)`
 - Finishes the communication

The process can be reversed with `DALocalToGlobal()`.

DA Local Function

The user provided function which calculates the nonlinear residual in 2D has signature

```
PetscErrorCode (*lfunc)(DALocalInfo *info, PetscScalar **x,  
                      PetscScalar **r, void *ctx)
```

info: All layout and numbering information

x: The current solution

- Notice that it is a multidimensional array

r: The residual

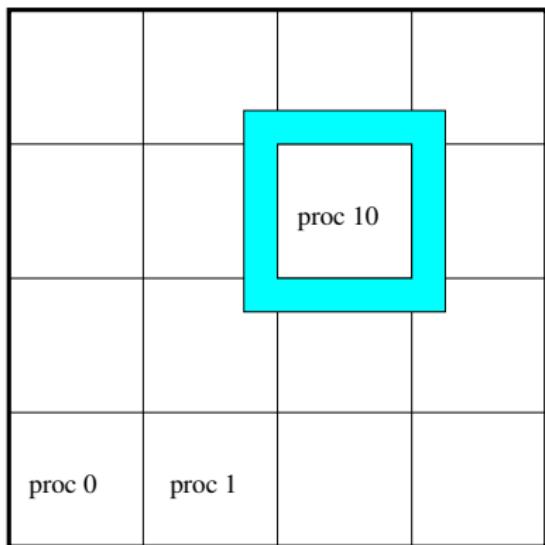
ctx: The user context passed to DASetLocalFunction()

The local DA function is activated by calling

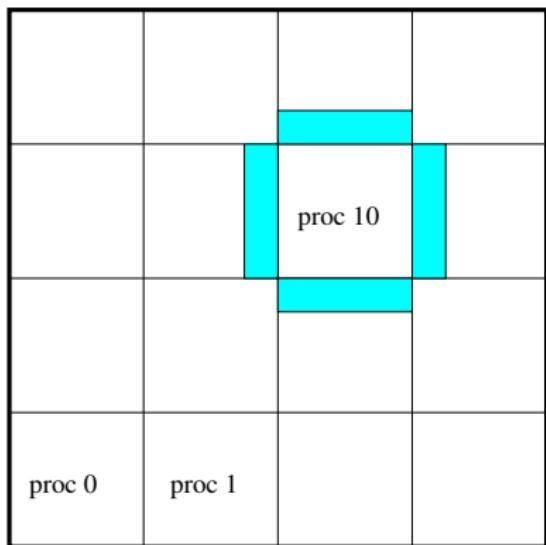
```
SNESSetFunction(snes, r, SNESDAFormFunction, ctx)
```

DA Stencils

Both the **box** stencil and **star** stencil are available.



Box Stencil



Star Stencil

Setting Values on Regular Grids

PETSc provides

```
MatSetValuesStencil(Mat A, m, MatStencil idxm[], n,
                    MatStencil idxn[], values[], mode)
```

- Each row or column is actually a MatStencil
 - This specifies grid coordinates and a component if necessary
 - Can imagine for unstructured grids, they are *vertices*
- The values are the same logically dense block in rows and columns

Code Update

Update to Revision 5

Structured Functions

- Functions takes values at the DA vertices
- Used as approximations to functions on the continuous domain
 - Values are really coefficients of linear basis
- User only constructs the local portion
- `make NP=2 EXTRA_ARGS="-test 1 -vec_view_draw -draw_pause -1" runbratu`

Code Update

Update to Revision 6

Sections

Sections associate data to submeshes

- Name comes from section of a fiber bundle
 - Generalizes linear algebra paradigm
- Define `restrict()`,`update()`
- Define `complete()`
- Assembly routines take a Topology and several Sections
 - This is called a Bundle

Section Types

Section can contain arbitrary values

- C++ interface is templated over value type
- C interface has three value types
 - SectionReal
 - SectionInt
 - SectionPair

Section can have arbitrary layout

- C++ interface can place unknowns on any Mesh entity (Sieve point)
- C interface has default layouts
 - `MeshGetVertexSectionReal()`
 - `MeshGetCellSectionReal()`

Viewing the Section

- `make EXTRA_ARGS="-test 1 -structured 0 -vec_view.vtk" runbratu`
 - Produces `linear.vtk` and `cos.vtk`
- Viewable with MayaVi, exactly as with the mesh.

Weak Forms

A *weak form* is the pairing of a function with an element of the *dual space*.

- Produces a number (by definition of the dual)
- Can be viewed as a “function” of the dual vector
- Used to define finite element solutions
- Require a dual space and integration rules

For example, for $f \in V$, we have the weak form

$$\int_{\Omega} \phi(\mathbf{x}) f(\mathbf{x}) dx \quad \phi \in V^*$$

Code Update

Update to Revision 7

FIAT Integration

Finite Element Integrator and Tabulator by Rob Kirby

<http://www.fenics.org/fiat>

The `quadrature.fiat` file contains:

- An element (usually a family and degree) defined by FIAT
- A quadrature rule

Then `make` produces `quadrature.h` with:

- Quadrature points and weights
- Basis function evaluations at the quadrature points
- Basis function derivative evaluations at the quadrature points

FIAT is part of the FEniCS project, as is the PETSc Sieve module

Code Update

Update to Revision 8

Viewing a DA Weak Form

- We use Q1 finite elements and a *Galerkin* formulation
 - Uses a linear basis in each dimension
 - Should really use a fast tensor evaluation routine
- Could substitute exact integrals for quadrature
- `make EXTRA_ARGS="-test 1 -vec_view_draw -draw_pause -1" runbratu`

Debugging Assembly

On two processes, I get a **SEGV!**

So we try running with:

- make NP=2 EXTRA_ARGS="-test 1 -vec_view_draw -draw_pause -1" debugbratu

Debugging Assembly

On two processes, I get a **SEGV!**

So we try running with:

- make NP=2 EXTRA_ARGS="-test 1 -vec_view_draw -draw_pause -1" debugbratu
- Spawns one debugger window per process

Debugging Assembly

On two processes, I get a **SEGV!**

So we try running with:

- make NP=2 EXTRA_ARGS="-test 1 -vec_view_draw -draw_pause -1" debugbratu
- Spawns one debugger window per process
- SEGV on access to ghost coordinates

Debugging Assembly

On two processes, I get a **SEGV!**

So we try running with:

- make NP=2 EXTRA_ARGS="-test 1 -vec_view_draw -draw_pause -1" debugbratu
- Spawns one debugger window per process
- SEGV on access to ghost coordinates
- Fix by using a local ghosted vector
 - Update to Revision 9

Debugging Assembly

On two processes, I get a **SEGV!**

So we try running with:

- make NP=2 EXTRA_ARGS="-test 1 -vec_view_draw -draw_pause -1" debugbratu
- Spawns one debugger window per process
- SEGV on access to ghost coordinates
- Fix by using a local ghosted vector
 - Update to Revision 9
- Notice that we were already using ghosted assembly
 - Could eliminate this by reorganizing element traversal

Code Update

Update to Revision 10

Section Assembly

First we do **local** operations:

- Loop over cells
- Compute cell geometry
- Integrate each basis function to produce an element vector
- Call `SectionUpdateAdd()`
 - Note that this updates the *closure* of the cell

Then we do **global** operations:

- `SectionComplete()` exchanges data across overlap
 - C just adds nonlocal values (C++ is flexible)
- C++ interface allow completion over arbitrary overlaps

```
make NP=2 EXTRA_ARGS="--test 1 -structured 0 -vec_view_vtk" runbratu
```

Global and Local

Local (analytical)

- Discretization/Approximation
 - FEM integrals
 - FV fluxes
- Boundary conditions

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Global (topological)

- Data management
 - Sections (local pieces)
 - Completions (assembly)
- Boundary definition
- Multiple meshes
 - Mesh hierarchies

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Largely dim independent
(e.g. mesh traversal)

Part IV

Defining an Operator

Update to Revision 11

- Evaluate again only the local portion
 - No nice local array form without copies
- Use MatSetValuesStencil() to convert (i, j, k) to indices
- Notice we use J^{-1} to convert derivatives
- `make NP=1 EXTRA_ARGS="-test 1 -mat_view_draw -draw_pause -1" runbratu`

DA Local Jacobian

The user provided function which calculates the nonlinear residual in 2D has signature

```
PetscErrorCode (*lfunc)(DALocalInfo *info, PetscScalar **x,  
                      Mat J, void *ctx)
```

info: All layout and numbering information

x: The current solution

J: The Jacobian

ctx: The user context passed to DASetLocalFunction()

The local DA function is activated by calling

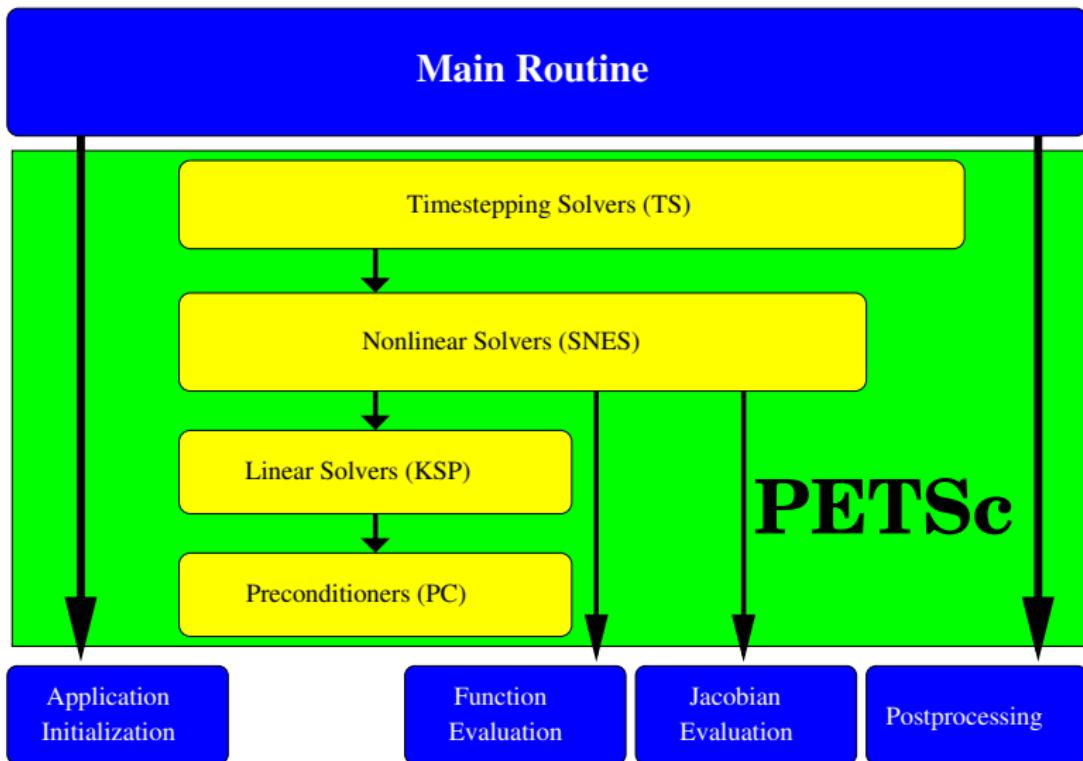
```
SNESSetJacobian(snes, J, J, SNESDAComputeJacobian, ctx)
```

- We evaluate the local portion just as with functions
- Currently updateOperator() uses MatSetValues()
 - We should properly have OperatorComplete()
 - Also requires a Section, for layout, and a global variable order
- `make NP=1 EXTRA_ARGS="-test 1 -structured 0 -mat_view_draw -draw_pause -1"`
`runbratu`

Part V

Solving Systems of Equations

Flow Control for a PETSc Application



The SNES interface is based upon callback functions

- SNESSetFunction()
- SNESSetJacobian()

When PETSc needs to evaluate the nonlinear residual $F(x)$, the solver calls the **user's** function inside the application.

The user function get application state through the `ctx` variable. PETSc never sees application data.

SNES Function

The user provided function which calculates the nonlinear residual has signature

```
PetscErrorCode (*func)(SNES snes, Vec x, Vec r, void *ctx)
```

x: The current solution

r: The residual

ctx: The user context passed to SNESSetFunction()

- Use this to pass application information, e.g. physical constants

SNES Jacobian

The user provided function which calculates the Jacobian has signature

```
PetscErrorCode (*func)(SNES snes, Vec x, Mat *J, Mat *M,  
                      MatStructure *flag, void *ctx)
```

x: The current solution

J: The Jacobian

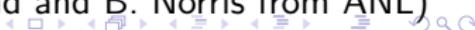
M: The Jacobian preconditioning matrix (possibly J itself)

ctx: The user context passed to SNESSetFunction()

- Use this to pass application information, e.g. physical constants
- Possible MatrStructure values are:
 - SAME_NONZERO_PATTERN, DIFFERENT_NONZERO_PATTERN,
 - ...

Alternatively, you can use

- a builtin sparse finite difference approximation
- automatic differentiation
 - AD support via ADIC/ADIFOR (P. Hovland and B. Norris from ANL)



- Line search strategies
- Trust region approaches
- Pseudo-transient continuation
- Matrix-free variants

Finite Difference Jacobians

PETSc can compute and explicitly store a Jacobian via 1st-order FD

- Dense
 - Activated by `-snes_fd`
 - Computed by `SNESDefaultComputeJacobian()`
- Sparse via colorings
 - Coloring is created by `MatFDColoringCreate()`
 - Computed by `SNESDefaultComputeJacobianColor()`

Can also use Matrix-free Newton-Krylov via 1st-order FD

- Activated by `-snes_mf` without preconditioning
- Activated by `-snes_mf_operator` with user-defined preconditioning
 - Uses preconditioning matrix from `SNESSetJacobian()`

Update to Revision 12

- DMMG supplies global residual and Jacobian to SNES
 - User supplies local version to DMMG
 - The `Rhs_*`() and `Jac_*`() functions in the example
- Allows automatic parallelism
- Allows grid hierarchy
 - Enables multigrid once interpolation/restriction is defined
- Paradigm is developed in unstructured work
 - Notice we have to scatter into contiguous global vectors (initial guess)
- Handle Neumann BC using `DMMGSetNullSpace()`

Part VI

Out of Flatland

Update to Revision 13

- Added new constructor call
- Added new local evaluation routines
 - `Rhs_Structured_3d()` and `Jac_Structured_3d()`
- Added new 3D source term

- Added new quadrature rule
- No need to change evaluation routines
 - Just need to pick the correct quadrature
- Added new 3D mesh files
 - Interfaces to TetGen (and soon TUMBLE) mesh generator

Part VII

The Undiscovered Country

What We Have Not Covered

- Unstructured hexes
- Nonlinearity
- Dirichlet BC
- Error Estimation
- Multigrid
- Semi-Lagrangian Schemes

References

- Documentation: <http://www.mcs.anl.gov/petsc/docs>
 - PETSc Users manual
 - Manual pages
 - Many hyperlinked examples
 - FAQ, Troubleshooting info, installation info, etc.
- Publications: <http://www.mcs.anl.gov/petsc/publications>
 - Research and publications that make use PETSc
- MPI Information: <http://www mpi-forum.org>
- **Using MPI** (2nd Edition), by Gropp, Lusk, and Skjellum
- **Domain Decomposition**, by Smith, Bjorstad, and Gropp

Proof is not currently enough to examine solvers

- N. M. Nachtigal, S. C. Reddy, and L. N. Trefethen, *How fast are nonsymmetric matrix iterations?*, SIAM J. Matrix Anal. Appl., **13**, pp.778–795, 1992.
- Anne Greenbaum, Vlastimil Ptak, and Zdenek Strakos, *Any Nonincreasing Convergence Curve is Possible for GMRES*, SIAM J. Matrix Anal. Appl., **17** (3), pp.465–469, 1996.